Name: _____

(1) If f(x) = 3x + 4, g(x) = 2x - 1, and $h(x) = x^2$, write a formula for $f \circ g \circ h$. What is the domain and range of this function?

SOLUTION:

$$(f \circ g \circ h)(x) = f(g(h(x)))$$

$$= f(g(x^{2}))$$

$$= f(2(x^{2}) - 1)$$

$$= f(2x^{2} - 1)$$

$$= 3(2x^{2} - 1) + 4$$

$$= 6x^{2} - 3 + 4$$

$$= 6x^{2} + 1.$$

The domain is all real numbers, and the range is $[1, \infty)$.

(2) Is the function $f(x) = \begin{cases} 2x + 6, & x \le -3 \\ x + 4, & x > -3 \end{cases}$ one-to-one? Why or why not?

SOLUTION: This function is one-to-one; the easiest way to see this is to note that its graph (pictured below) passes the horizontal line test.

