


The theorem from lecture, that you can tile any $2^n \times 2^n$ checkerboard minus one square with -shaped tiles, is NOT true for $2^n \times 2^n$ checkerboards!
Can you find a counterexample?

Some additional facts you could try to prove using induction:

$$1) \text{ For } n \geq 1, \quad \sum_{i=1}^n 2^i = 2^{n+1} - 2.$$

$$2) \text{ For } n \geq 1, \quad \sum_{i=1}^n i(i+1) = \frac{n(n+1)(n+2)}{3}.$$

$$3) \text{ For } n \geq 5, \quad 4n < 2^n.$$

$$4) \text{ For } n \geq 1, \quad 8^n - 3^n \text{ is divisible by } 5.$$

If you are interested in hearing more about Lie algebras on Saturday, talk to me after class on Thursday!