

Reading. §§3.5–3.7.

Problems from the book: the starred problems may be carefully graded. You will be given a “completeness” score, depending on how carefully you complete these problems.

- §3.3: 5, 6*, 9, 13
- §3.4: 8, 11
- §3.5: 15, 17, 14*
- §3.6: 6*

Additional problems: These will be carefully graded!

1. Suppose V and W are vector spaces over \mathbb{R} . Show that the set of linear transformations

$$\mathcal{L}(V, W) = \{T : V \rightarrow W \mid T \text{ is linear}\},$$

is itself a vector space over \mathbb{R} .

2. Suppose that $f : \mathbb{R}^2 \rightarrow \mathbb{R}$ satisfies Laplace’s equation $D_1^2 f + D_2^2 f = 0$. True or false: the function

$$g \left(\begin{array}{c} x \\ y \end{array} \right) = f \left(\begin{array}{c} \frac{x}{x^2+y^2} \\ \frac{y}{x^2+y^2} \end{array} \right)$$

also satisfies Laplace’s equation. Prove this, or give a counterexample.