

Prove the comparison theorem for improper integrals of the second kind: If $|f(x)| \leq g(x)$ on $(a, b]$ and if g is integrable on $(a, b]$, then f is also integrable on $(a, b]$.