

1. (a) Based on your pre-class activity reflections, what should the definition of $\lim_{x \rightarrow \infty} f(x)$ “look like”?

(b) And what about the definition of $\lim_{x \rightarrow -\infty} f(x)$?

(c) What are the key elements of this definition?

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2. Compute the limits as x goes to infinity and negative infinity for the following functions:

$$(a) f(x) = \frac{2x^4 + 2x^2 - 3}{3x^4 + x^3 - 2x^2}$$

$$(b) g(x) = \frac{2x^5 + 2x^2 - 3}{3x^4 + x^3 - 2x^2}$$

$$(c) h(x) = \frac{2x^4 + 2x^2 - 3}{3x^6 + x^3 - 2x^2}$$

$$(d) j(x) = \frac{\sqrt{2x^6 + 2x^2 - 3}}{3x^3 - 2x^2}$$

3. Compute the horizontal asymptotes of the following functions:

(a) $f(x) = \frac{\sqrt[3]{x} - 4x + 7}{3x + x^{2/3} - 1}$

(b) $g(x) = \frac{1}{x} \sin x$ (compare your answer with $\lim_{x \rightarrow \infty} \sin(\pi x)$ that you computed in the pre-class activity).

(c) $f(x) = \frac{-x^2 + 5x - 1}{2x + 3}$

4. Compute the following limits:

(a) $\lim_{x \rightarrow \infty} (x^2 - x)$

(b) $\lim_{x \rightarrow \infty} (\sqrt{x^2 + 2} - x)$

(c) $\lim_{x \rightarrow \infty} (\sqrt{x^2 + ax} - \sqrt{x^2 + bx})$, where a and b are constants

Based on what you have just computed, can you find a limit for which “ $\infty - \infty$ ” gives 3? What about 10? What about any other number?

5. Determine the vertical and horizontal asymptotes of the following functions:

(a) $f(x) = \frac{2x^2 + 1}{3x - 5}$

(b) $f(x) = \frac{2x^2 + 5}{x^2 - 5x}$