

1. Using the computations you have done in the pre-class activity as well as the Limit Laws (Theorem 1, p. 66), compute the following limits. For and justify each step of your computations.

(a)  $\lim_{x \rightarrow 1} \frac{x^2 + x - 2}{x - 2},$

(b)  $\lim_{x \rightarrow 1} \frac{x^2 + x - 2}{x - 1},$

(c)  $\lim_{h \rightarrow 0} \frac{\sqrt{7h + 9} - 3}{h},$

(d)  $\lim_{t \rightarrow -1} \frac{t^2 + 3t + 2}{t^2 - 1},$

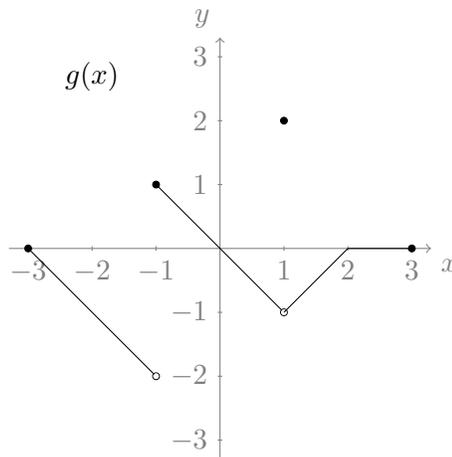
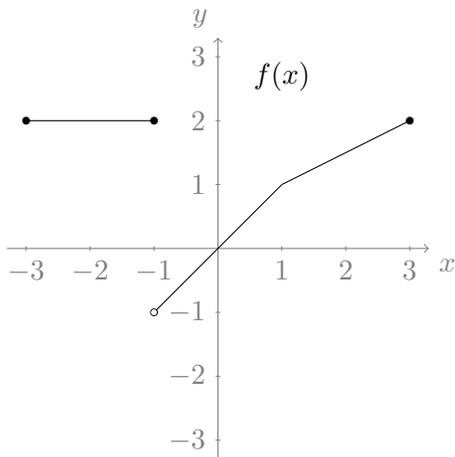
(e)  $\lim_{x \rightarrow -2} \frac{x + 2}{\sqrt{x^2 + 5} - 3},$

*Here point out the step where we “simplify the fractions” and explain why the whole process works (thus making the link with the pre-class activity and graphs the students drew). Also point out that we could NOT have plugged the numbers in at the very start.*

*OVERALL, make sure to address the following questions/topics at some point:*

- Why can we sometime just plug in the value in the limit and at other times not?*
- What is the difference between the left-hand and right-hand limit?*
- Make sure the students can explain in words what is happening when computing limits.*

2. Here are the graphs of the functions  $f$  and  $g$ . Compute the limits indicated below.



(a)  $\lim_{x \rightarrow 1} g(x)$  *lim g(x) ≠ g(a)*

(b)  $g(1)$  *lim g(x) ≠ g(a)*

(c)  $\lim_{x \rightarrow -1} f(x)$  *DNE*

(d)  $\lim_{x \rightarrow -2} \frac{f(x)}{g(x)}$  *the limit exists*

(e)  $\lim_{x \rightarrow 1} \frac{f(x)}{g(x)}$  *lim f(x)/g(x) ≠ f(a)/g(a)*

(f)  $\lim_{x \rightarrow 0} \frac{f(x)}{g(x)}$  *lim f(x)/g(x) exists even though g(x) (and f(x)) go to 0*

(g)  $\lim_{x \rightarrow 2} \frac{f(x)}{g(x)}$  *the left-hand limit goes to infinity and the right-hand limit is undefined*

(h)  $\lim_{x \rightarrow -1} \frac{f(x)}{g(x)}$  *the limit exists even though the individual limits do not*

*Make sure to have defined what going to infinity means for a limit.*

3. Compute the following limits. If a limit does not exist because the right-hand and left-hand limits differ, evaluate them separately.

$$\text{a) } \lim_{x \rightarrow 1} \frac{x^2 + 3x + 2}{(x - 1)^2} \quad \text{b) } \lim_{x \rightarrow 1} \frac{x^2 + 3x + 2}{x - 1}$$

*Underline that for a) the limit goes to infinity whereas for b) it depends from which side one comes.*

4. Compute the following limits using the definition and/or the limit laws. Drawing the graphs of the functions may be helpful here.

(a)  $\lim_{x \rightarrow 0} \sin(1/x)$ , *DNE, the graph of this function is on Worksheet 1.*

(b)  $\lim_{x \rightarrow 0} x \sin(1/x)$ . *Don't let students work too long on this one.*

*Underline why the limit laws does NOT apply here.*

*Use the graph of the function as a motivation for the Squeeze Theorem and then formally introduce the theorem.*