

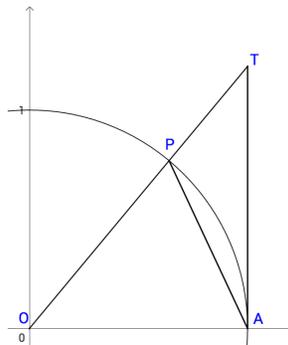
The Squeeze Theorem is another way to compute limits, often employed when limit laws cannot be used.

1a) Explain why you cannot use limit laws to determine the limits  $\lim_{t \rightarrow 0} t^2 \sin\left(\frac{1}{t}\right)$  and  $\lim_{t \rightarrow 0} \left|t \cos\left(\frac{1}{t}\right)\right|$ ?

1b) Explain how you would use the squeeze theorem to compute the limit of  $\lim_{t \rightarrow 0} t^2 \sin\left(\frac{1}{t}\right)$ .

1c) Explain how you would use the squeeze theorem to compute the limit of  $\lim_{t \rightarrow 0} \left|t \cos\left(\frac{1}{t}\right)\right|$ .

In this section, we will compute the limit  $\lim_{t \rightarrow 0} \frac{\sin t}{t}$ . In order to do so, we will use a geometrical argument (and the figure below).



2a) The figure above represents the unit circle and a given angle  $t$ . Determine and rank the areas of: i) the triangle OPA, ii) the area sector OPA, and iii) the triangle OTA.

2b) How can you use this relation to compute the limit  $\lim_{t \rightarrow 0} \frac{\sin t}{t}$ ? What limit laws or theorem have you used?

2c) Write a solution detailing how to compute the limit  $\lim_{t \rightarrow 0} \frac{\sin t}{t}$ .