

1. Last time we saw that as a consequence of the Mean Value Theorem, for a differentiable function  $f(x)$ :

if  $f'(x) > 0$  then the functions is ...

if  $f'(x) < 0$  then the functions is ...

Based on this observation, we can formulate the **First Derivative Test** (p. 239 in Thomas):

If  $c$  is a critical point of a differentiable function and :

- if  $f'(x)$  changes from negative to positive at  $c$ , then  $c$  is
- if  $f'(x)$  changes from positive to negative at  $c$ , then  $c$  is
- if  $f'(x)$  does not change sign at  $c$ , then  $c$  is

2. Let us see an application of the First Derivative Test

(a) Consider the function  $f(x) = x^3 - 5x^2 + 8x - 4$ .

i. What are the critical points?

ii. On what intervals is  $f(x)$  increasing or decreasing?

iii. What are the local maxima and minima of  $f(x)$  (if they exist)? Give their coordinates.

iv. What are the global maxima and minima of  $f(x)$  (if they exist)? Give their coordinates.

- (b) Same questions but for  $f(x)$  defined on the interval  $[-3, 3]$ .  
What changes and what remains the same?