REVIEW Math 1920 - Andres Fernandez NAME:

October 27, 2018

Problems

- (1) Do the following limit problems:
 - (a) Let $a, b \ge 0$. Show that the limit

$$\lim_{(x,y)\to(0,0)}\frac{x^ay^b}{x^2+y^2}$$

is 0 if a, b > 2 and does not exist if $a + b \le 2$.

(b) Determine whether the following limit exists or not:

$$\lim_{(x,y)\to(0,0)}\frac{x^3y^2+x^2y^3}{x^4+y^4}$$

- (2) How does the surface described in spherical coordinates by $\rho^2(1 + A\cos^2(\phi)) = 1$ change with the constant A.
- (3) Find the parametrization of the intersection of the surfaces $x^2 + y^2 = 3$ and $z^3 6y + 4x = 17$. Set up an integral for the arclength of the curve.
- (4) Find f such that:

(a)
$$\frac{\partial}{\partial x}f = 6x^2y$$
, and $\frac{\partial}{\partial y}f = 2x^3 - 3$

(b)
$$\frac{\partial}{\partial x}f = e^x - y\sin(xy)$$
, and $\frac{\partial}{\partial y}f = -x\sin(xy) + 5y^4$

- (5) Parametrize by arclength the helix $r(t) = \langle 4\cos(5t), 4\sin(5t), 3t \rangle$
- (6) Consider the sphere $x^2 + y^2 + z^2 = 30$. When is the tangent plane parallel to the plane 3x 5y + 7z = 8?