## REVIEW

## MATH 1910 Recitation August 30, 2016

§5.1 (Approximating and Computing Area); §5.2 (The definite integral)

(1) Approximations to the area under the graph of f over the interval [a, b]:

Right-endpoint	Left-endpoint	Midpoint
$R_N = \Delta x \sum_{j=1}^{\infty} f(x_j)$	$L_N = \Delta x \sum_{j=-}^{(4)} f(x_j)$	$M_N = \Delta x \sum_{j=0}^{N-1} $ (5)

(2) If f is continuous on [a, b], then the area A under the graph y = f(x) is defined as

$$A :=$$
  $(6)$ 

- (3) The **definite integral** is the of the region between the graph of f and the x-axis. If f is on [a,b], then f is integrable over [a,b].
- (4) Some properties of definite integrals:

(a) 
$$\int_{a}^{b} (f(x) + g(x)) dx =$$

(b) 
$$\int_a^b Cf(x)dx = \begin{bmatrix} 100 \\ 100 \end{bmatrix}$$

(c) 
$$\int_{a}^{b} f(x)dx = -\int_{b}^{a} f(x)dx$$

(d) 
$$\int_{a}^{b} f(x)dx + \int_{b}^{c} f(x)dx =$$

(5) Some formulas for computing integrals

(a) 
$$\int_a^b C dx =$$

(b) 
$$\int_{0}^{b} x dx =$$
 (13)

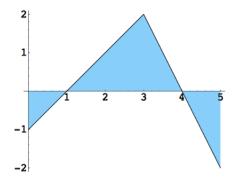
(c) 
$$\int_0^b x^2 dx =$$
 (14)

(6) **Comparison Theorem:** If  $f(x) \le g(x)$  on [a,b], then  $\int_a^b f(x) dx$   $\int_a^b g(x) dx$ .

## PRACTICE PROBLEMS

§5.1 (Approximating and Computing Area); §5.2 (The definite integral)

(1) Use the graph of g(x) given below to evaluate the following integrals.



- (a)  $\int_0^3 g(x) \, dx$
- (b)  $\int_3^5 g(x) \, dx$
- (c)  $\int_0^5 g(x) \, dx$
- (2) Find a formula for  $R_N$  for  $f(x) = 3x^2 x + 4$  over the interval [0,1].
- (3) Calculate  $\int_{2}^{5} (2x+1) dx$  in three ways:
  - (a) As a limit  $\lim_{N\to\infty} R_N$ .
  - (b) Using geometry, interpreting this as the area under a graph.
  - (c) Using the properties of the integral.
- (4) Use the basic properties of the integral to calculate the following.
  - (a)  $\int_{1}^{4} 6x^2 dx$
  - (b)  $\int_{-2}^{3} (3x+4) dx$
  - (c)  $\int_{1}^{3} |2x-4| dx$
- (5) Evaluate  $\lim_{N\to\infty}\frac{1}{N}\sum_{j=1}^N\sqrt{1-\left(\frac{j}{N}\right)^2}$  by interpreting the limit as an area.