Torus Glued Comparison of Level 2 Eigenfunctions and Level 1 Eigenfunctions By Averaging

SPUR 2016

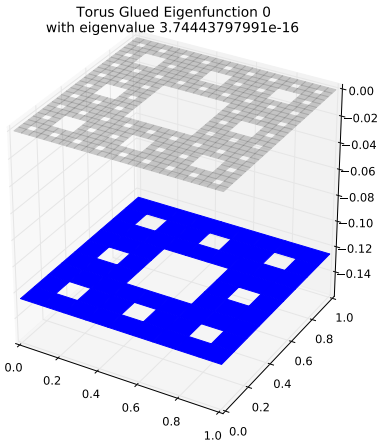
May 23, 2018

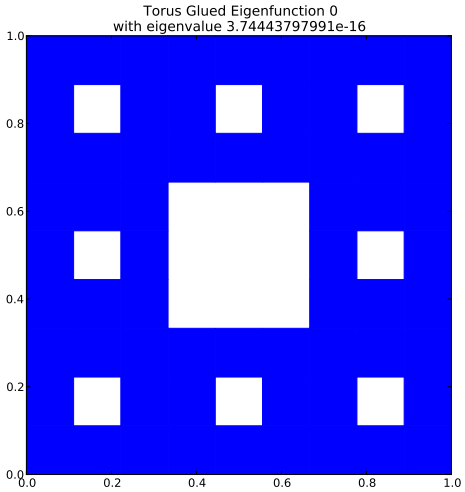
Key to Dot Value

Dot values are in general between 0 and 1; those close to 0 are better matches, while those close to 1 are not good matches. Dot value 2 indicates the eigenvalue averages to the zero function. Dot value 3 indicates the projection onto the closest eigenspace is zero.

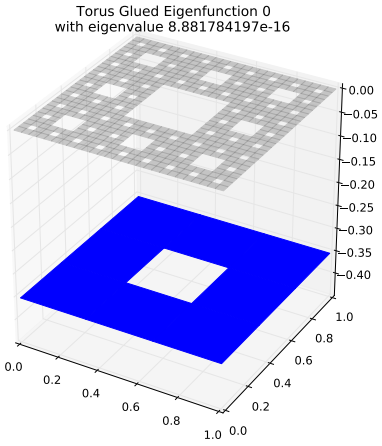
1 $M = 2$ Eigenfunction 0

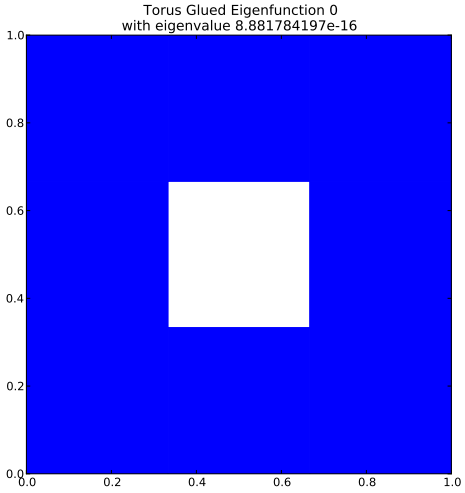
$M = 2$ Eigenfunction 0 has eigenvalue 3.74443797991e-16





Compare to $m = 1$ eigenspace with eigenvalue 8.881784197e-16

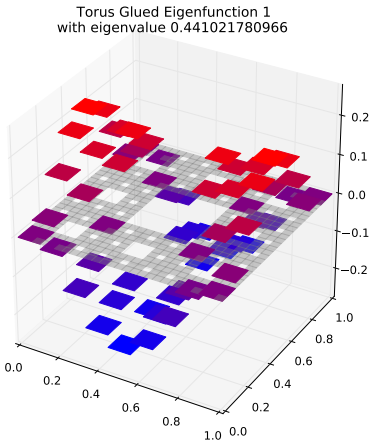


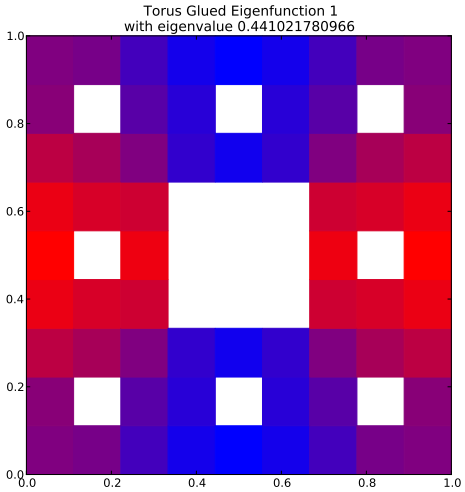


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 0.421586237276$
Dot Value: 0.0

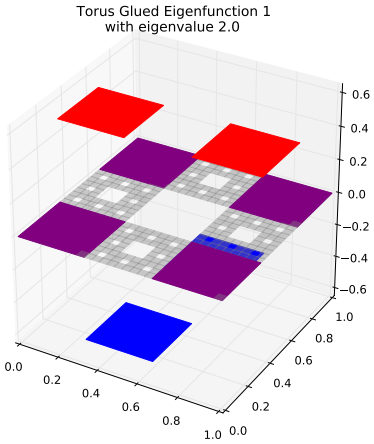
2 $M = 2$ Eigenfunction 1

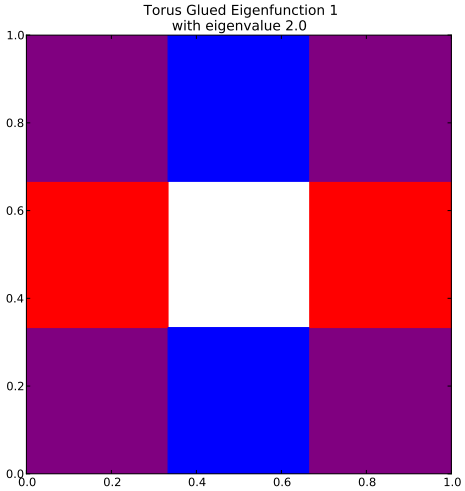
$M = 2$ Eigenfunction 1 has eigenvalue 0.441021780966





Compare to $m = 1$ eigenspace with eigenvalue 2.0

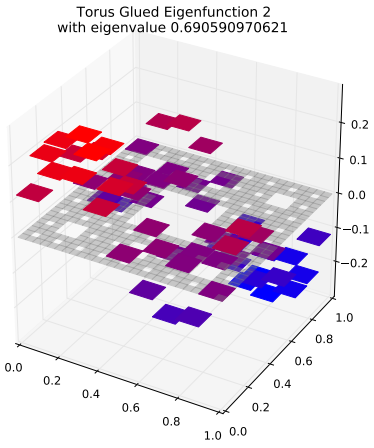


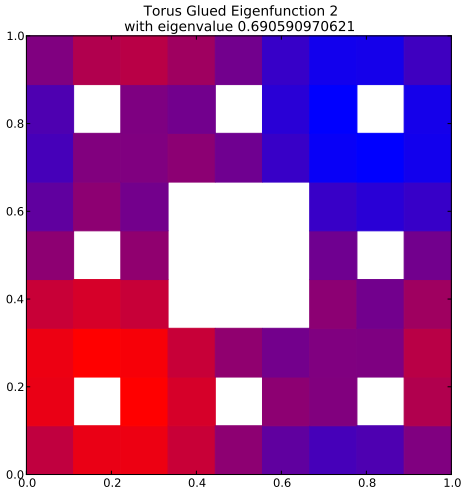


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 0.220510890483$
Dot Value: 1.1102230246251565e-16

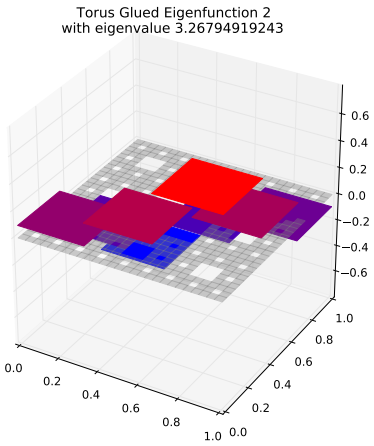
3 $M = 2$ Eigenfunction 2

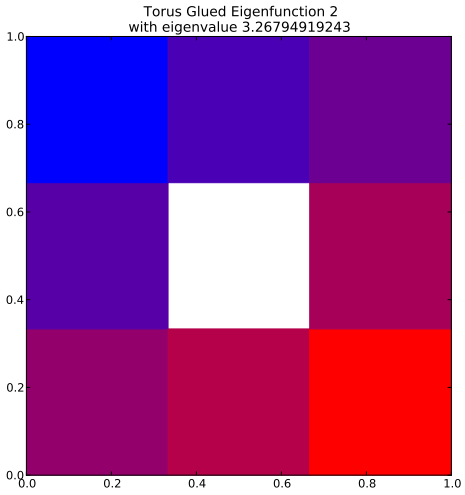
$M = 2$ Eigenfunction 2 has eigenvalue 0.690590970621





Compare to $m = 1$ eigenspace with eigenvalue 3.26794919243
(Note: Eigenspace Dimension > 1)

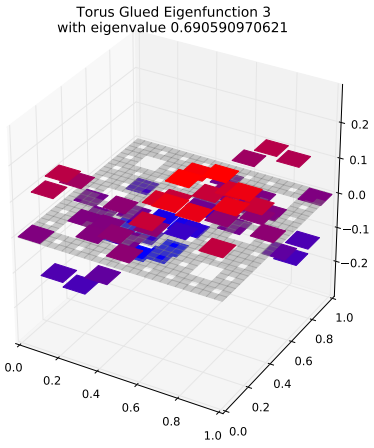


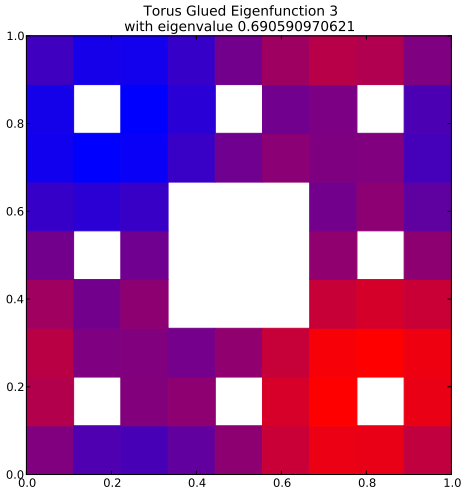


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 0.211322431885$
Dot Value: 0.0072084228188636 91

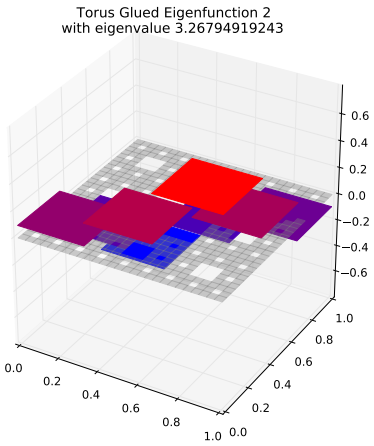
4 $M = 2$ Eigenfunction 3

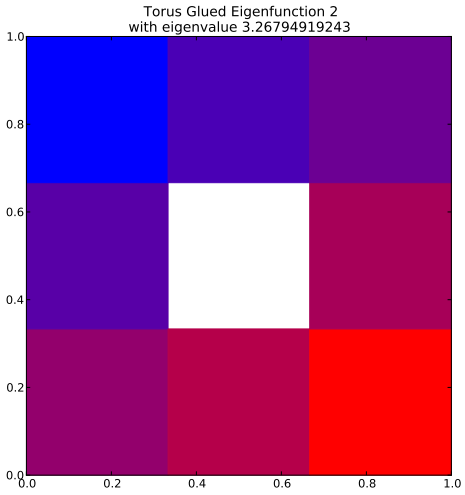
$M = 2$ Eigenfunction 3 has eigenvalue 0.690590970621





Compare to $m = 1$ eigenspace with eigenvalue 3.26794919243
(Note: Eigenspace Dimension > 1)

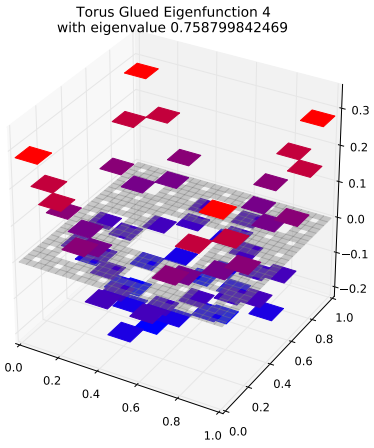


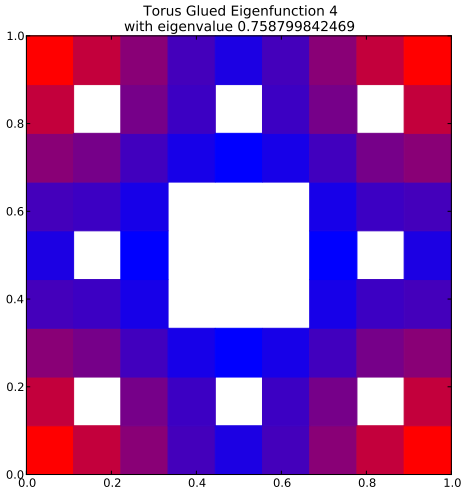


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 0.211322431885$
Dot Value: 0.0072084228188634 69

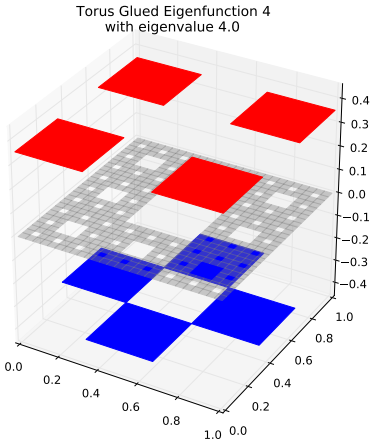
5 $M = 2$ Eigenfunction 4

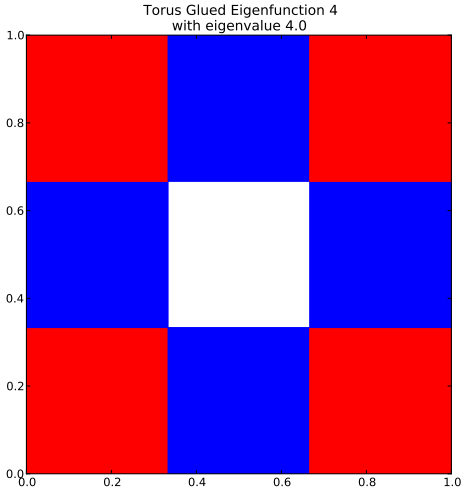
$M = 2$ Eigenfunction 4 has eigenvalue 0.758799842469





Compare to $m = 1$ eigenspace with eigenvalue 4.0

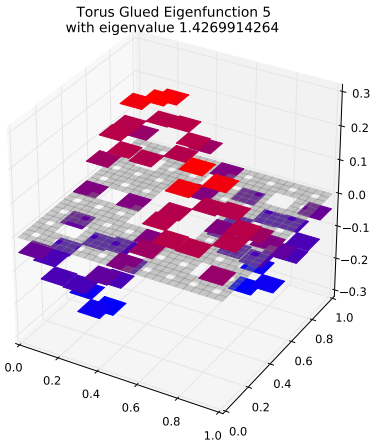


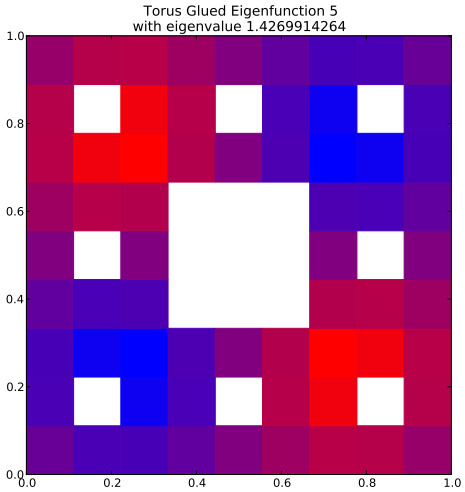


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 0.189699960617$
Dot Value: 2.220446049250313e-16

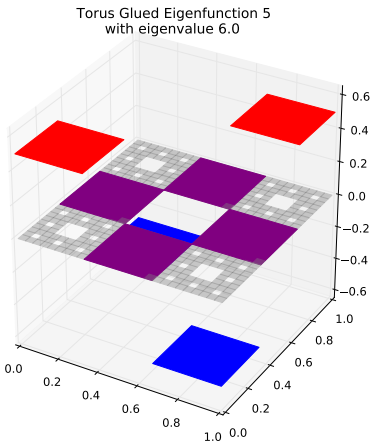
6 $M = 2$ Eigenfunction 5

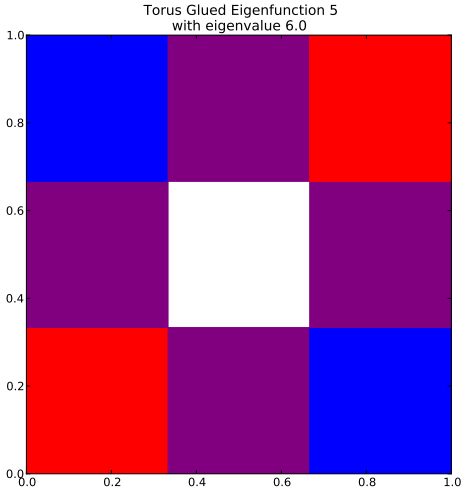
$M = 2$ Eigenfunction 5 has eigenvalue 1.4269914264





Compare to $m = 1$ eigenspace with eigenvalue 6.0

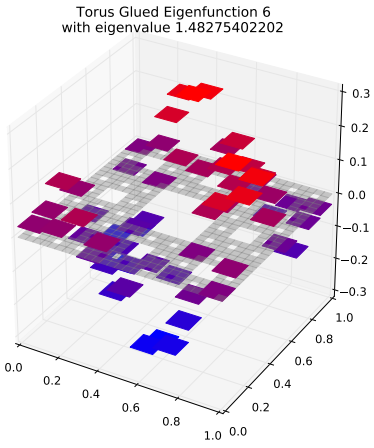


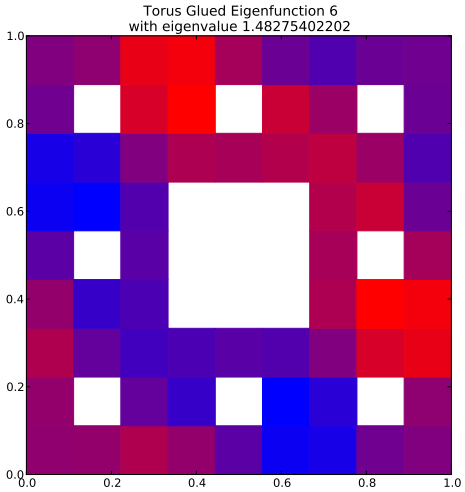


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 0.237831904401$
Dot Value: 2.220446049250313e-16

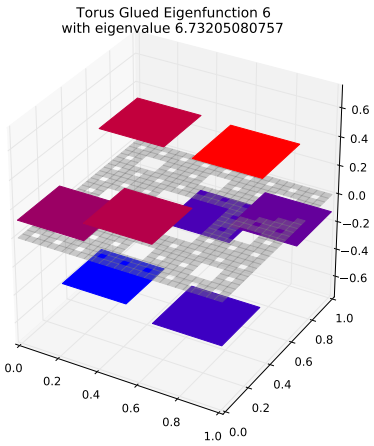
7 $M = 2$ Eigenfunction 6

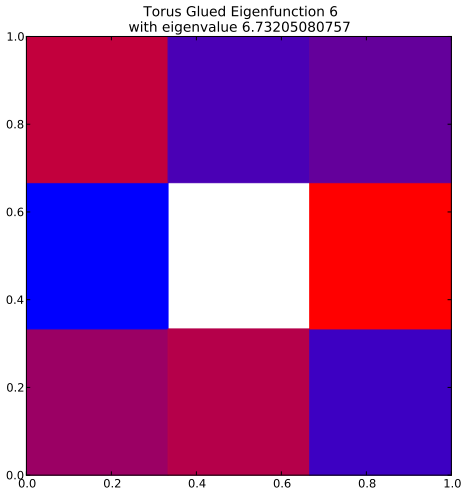
$M = 2$ Eigenfunction 6 has eigenvalue 1.48275402202





Compare to $m = 1$ eigenspace with eigenvalue 6.73205080757
(Note: Eigenspace Dimension > 1)

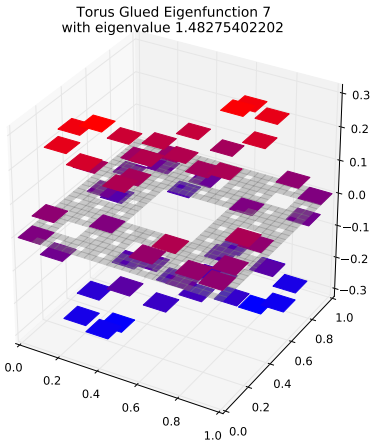


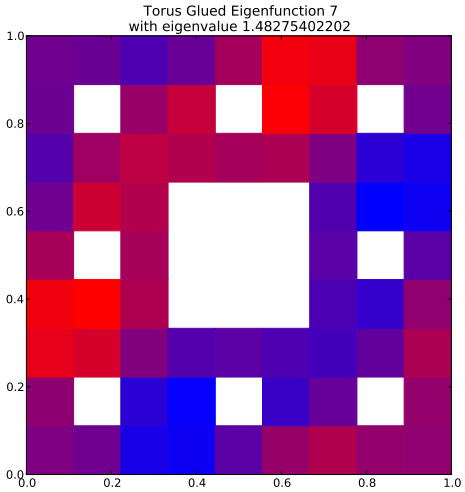


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 0.220252945856$
Dot Value: 0.08916117818499303

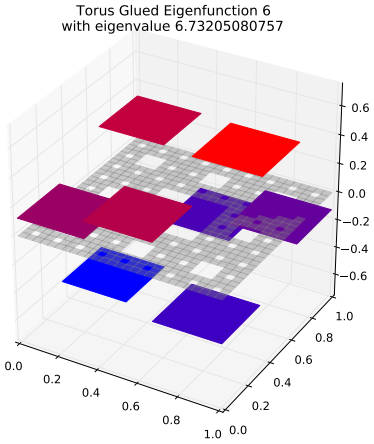
8 $M = 2$ Eigenfunction 7

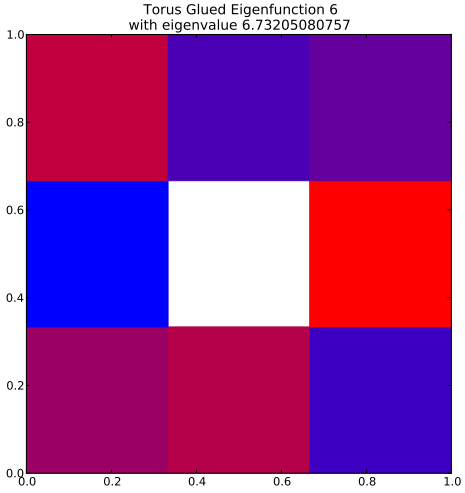
$M = 2$ Eigenfunction 7 has eigenvalue 1.48275402202





Compare to $m = 1$ eigenspace with eigenvalue 6.73205080757
(Note: Eigenspace Dimension > 1)

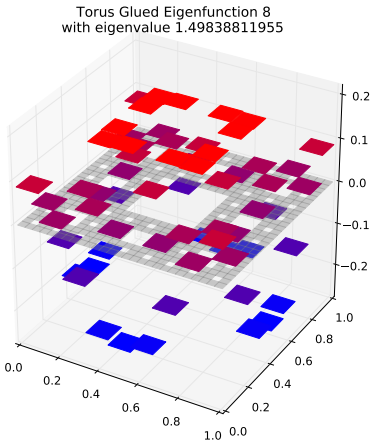


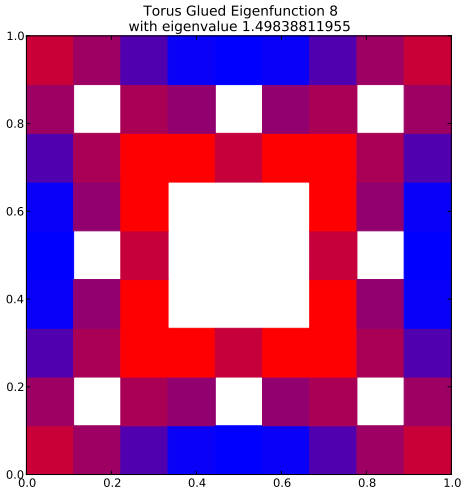


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 0.220252945856$
Dot Value: 0.0891611781849927

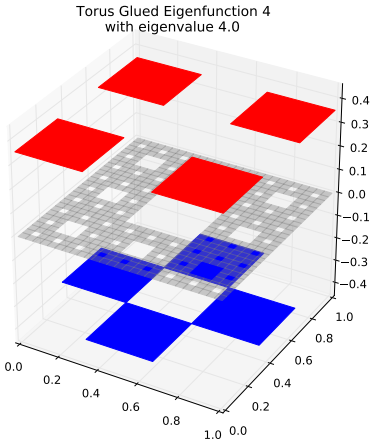
9 $M = 2$ Eigenfunction 8

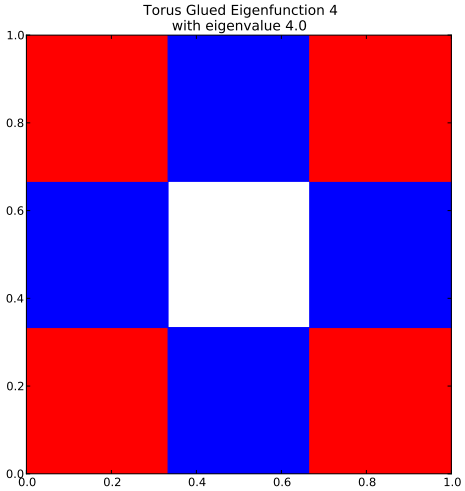
$M = 2$ Eigenfunction 8 has eigenvalue 1.49838811955





Compare to $m = 1$ eigenspace with eigenvalue 4.0

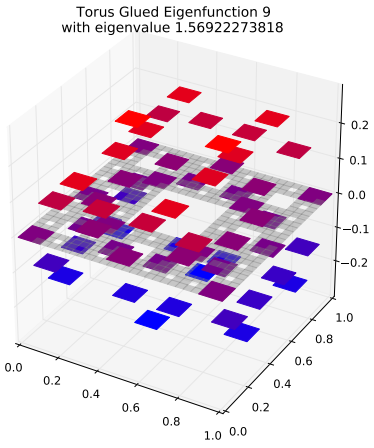


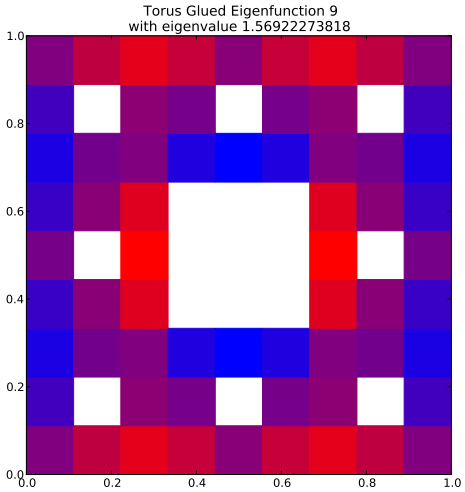


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 0.374597029888$
Dot Value: 2.220446049250313e-16

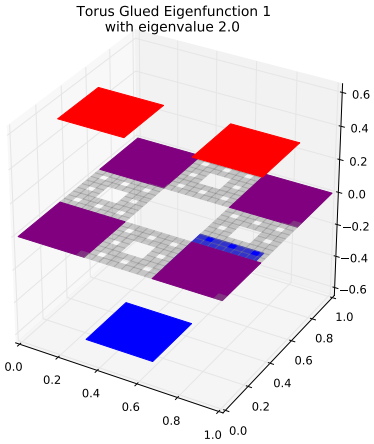
10 $M = 2$ Eigenfunction 9

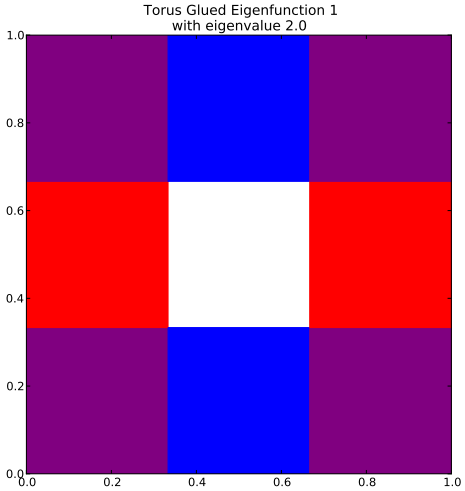
$M = 2$ Eigenfunction 9 has eigenvalue 1.56922273818





Compare to $m = 1$ eigenspace with eigenvalue 2.0

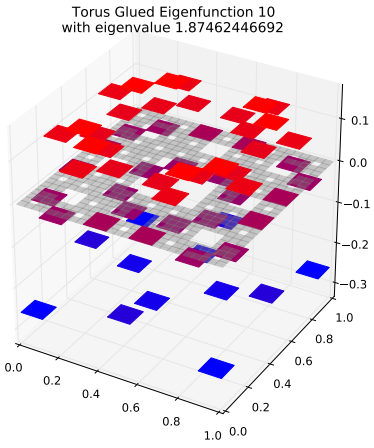


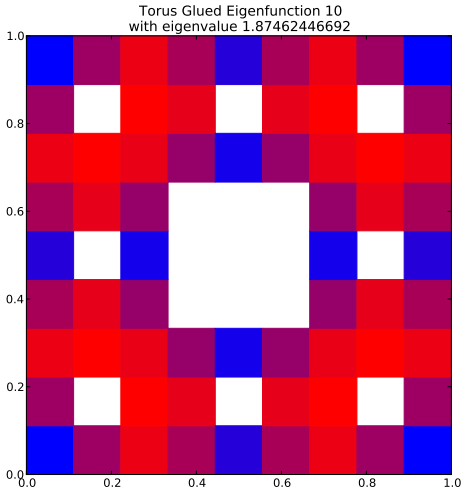


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 0.78461136909$
Dot Value: 1.1102230246251565e-16

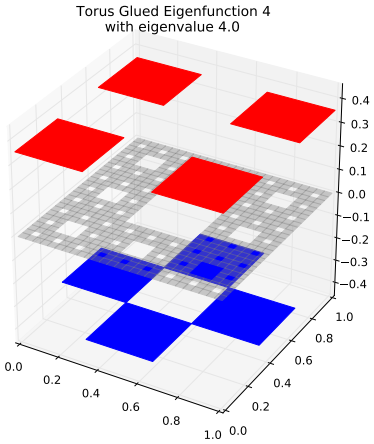
11 $M = 2$ Eigenfunction 10

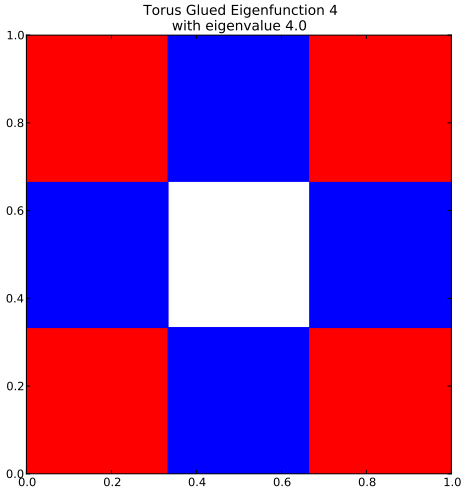
$M = 2$ Eigenfunction 10 has eigenvalue 1.87462446692





Compare to $m = 1$ eigenspace with eigenvalue 4.0

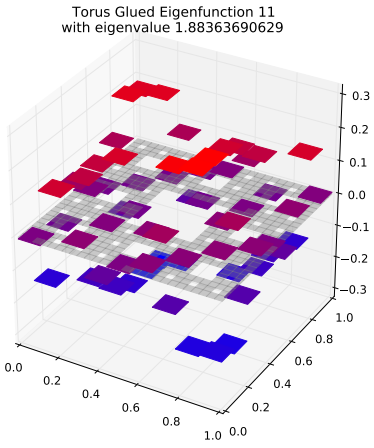


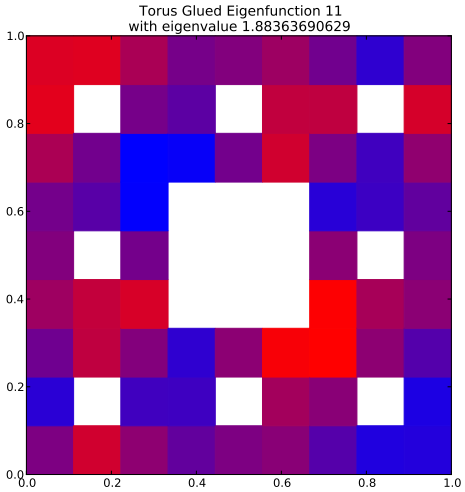


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 0.468656116731$
Dot Value: 0.0

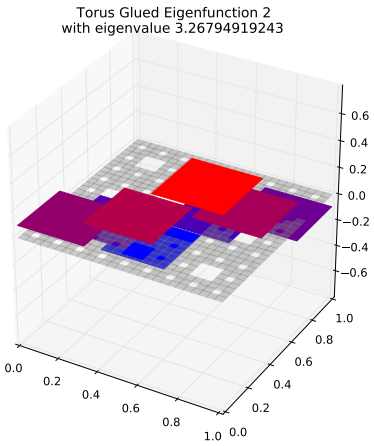
12 $M = 2$ Eigenfunction 11

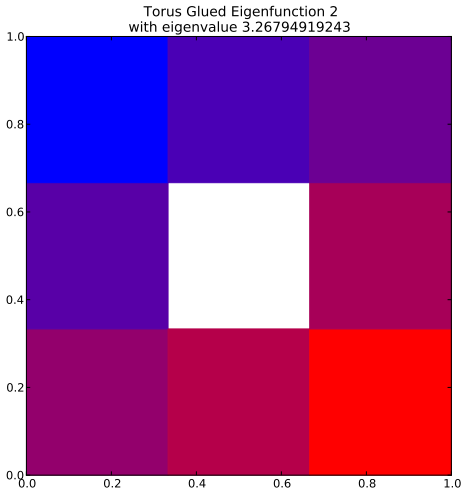
$M = 2$ Eigenfunction 11 has eigenvalue 1.88363690629





Compare to $m = 1$ eigenspace with eigenvalue 3.26794919243
(Note: Eigenspace Dimension > 1)

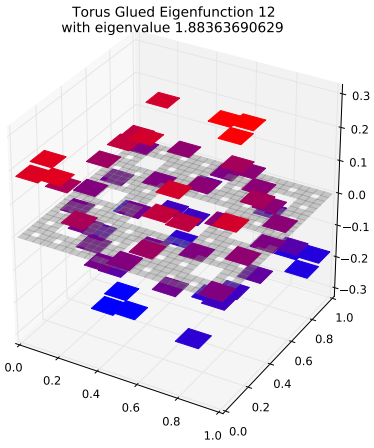


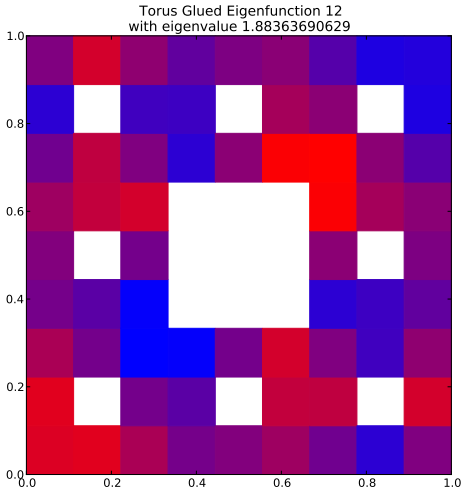


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 0.576397243462$
Dot Value: 0.1131236807071937

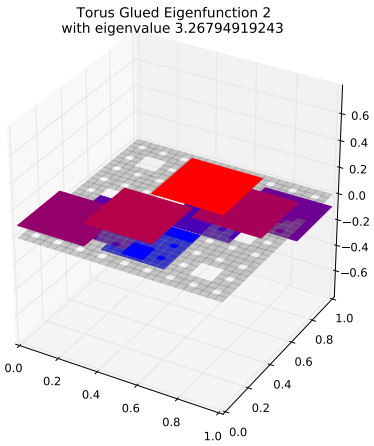
13 $M = 2$ Eigenfunction 12

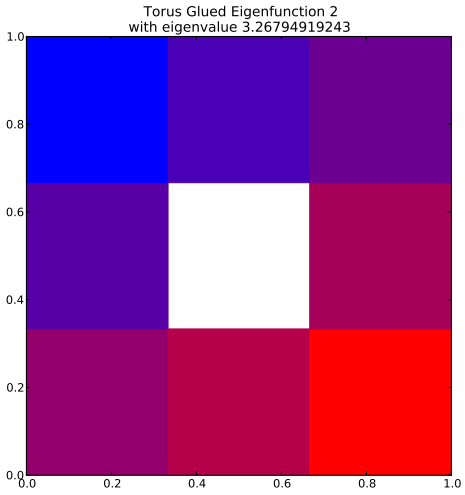
$M = 2$ Eigenfunction 12 has eigenvalue 1.88363690629





Compare to $m = 1$ eigenspace with eigenvalue 3.26794919243
(Note: Eigenspace Dimension > 1)

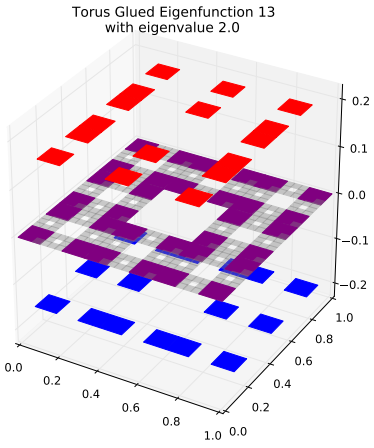


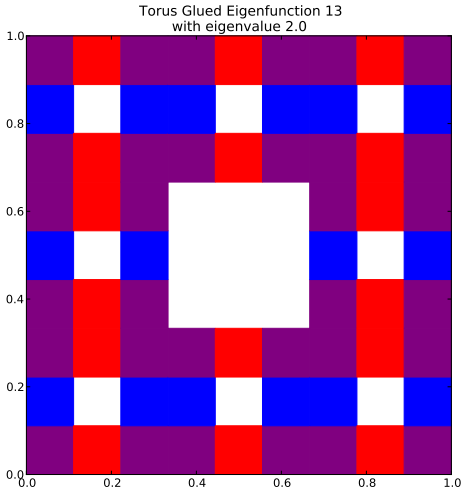


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 0.576397243462$
Dot Value: 0.11312368070719725

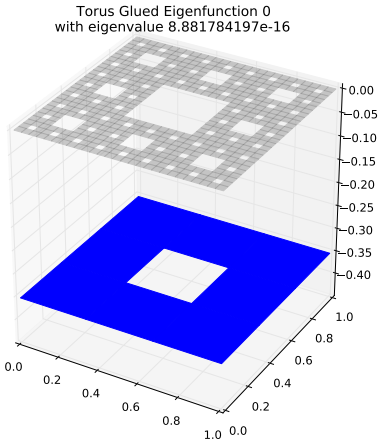
14 $M = 2$ Eigenfunction 13

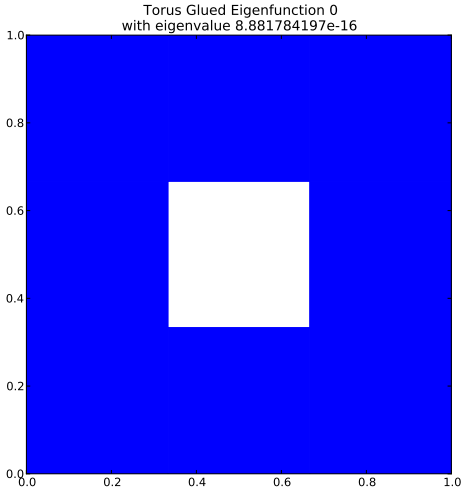
$M = 2$ Eigenfunction 13 has eigenvalue 2.0





Compare to $m = 1$ eigenspace with eigenvalue 8.881784197e-16

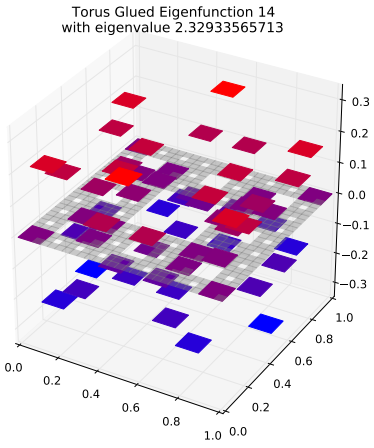


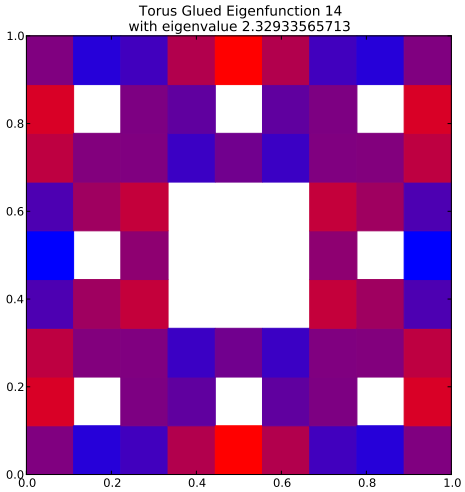


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 2.25179981369e + 15$
Dot Value: 2

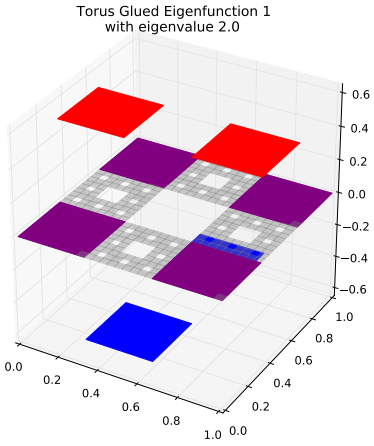
15 $M = 2$ Eigenfunction 14

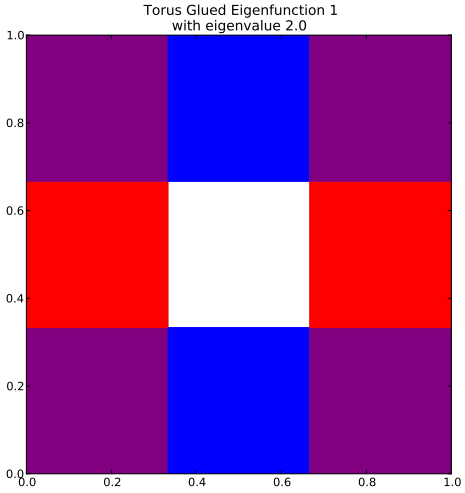
$M = 2$ Eigenfunction 14 has eigenvalue 2.32933565713





Compare to $m = 1$ eigenspace with eigenvalue 2.0

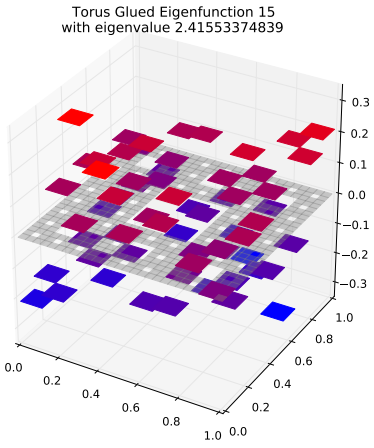


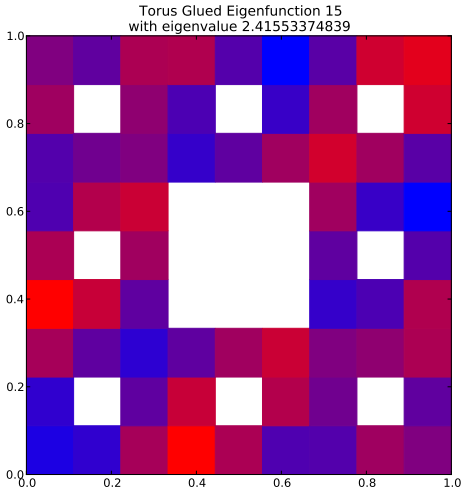


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 1.16466782857$
Dot Value: 2.220446049250313e-16

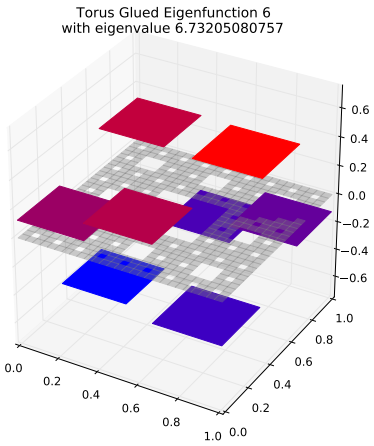
16 $M = 2$ Eigenfunction 15

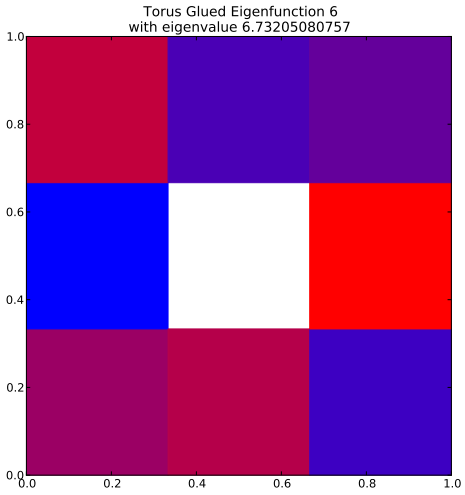
$M = 2$ Eigenfunction 15 has eigenvalue 2.41553374839





Compare to $m = 1$ eigenspace with eigenvalue 6.73205080757
(Note: Eigenspace Dimension > 1)

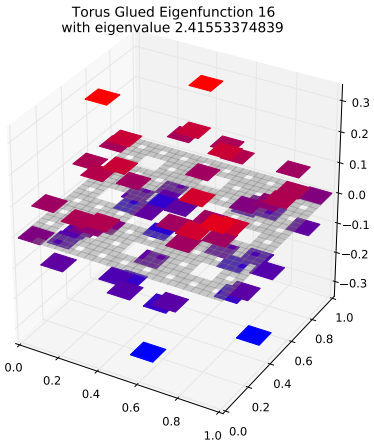


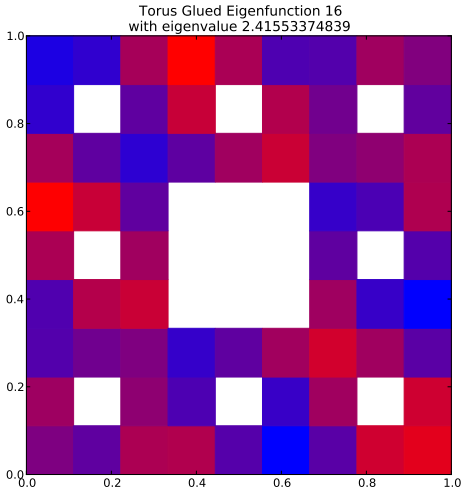


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 0.358810980106$
Dot Value: 0.011440672902887528

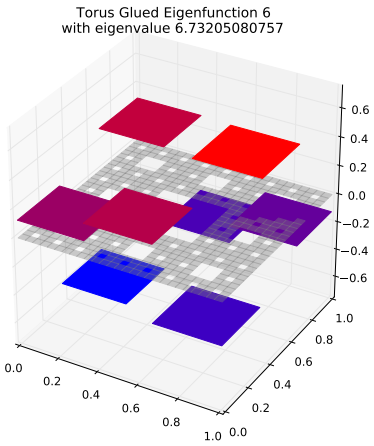
17 $M = 2$ Eigenfunction 16

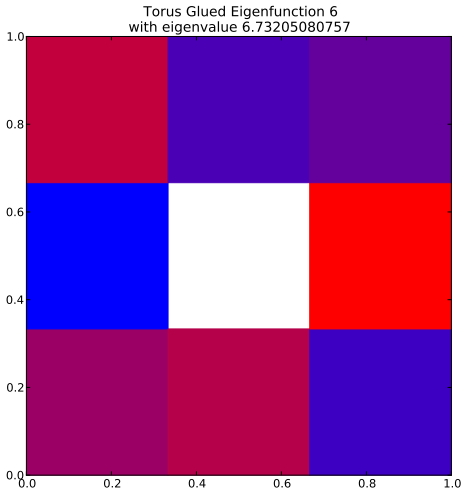
$M = 2$ Eigenfunction 16 has eigenvalue 2.41553374839





Compare to $m = 1$ eigenspace with eigenvalue 6.73205080757
(Note: Eigenspace Dimension > 1)

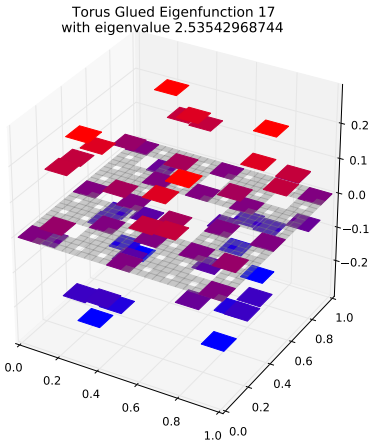


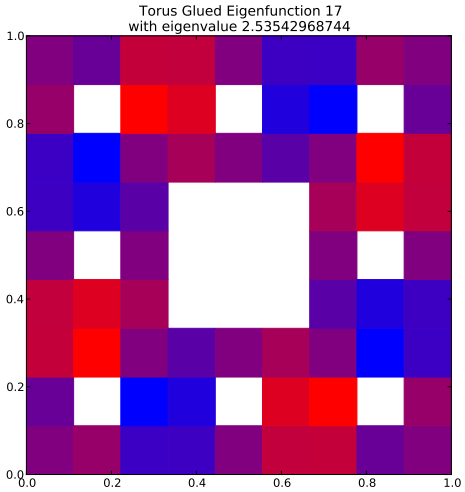


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 0.358810980106$
Dot Value: 0.011440672902887417

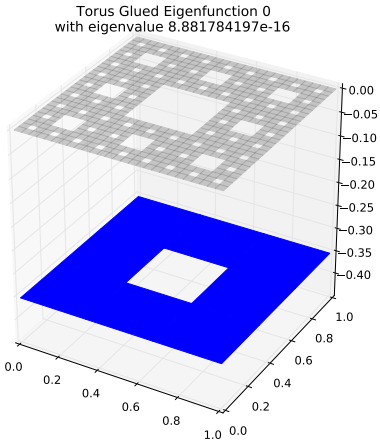
18 $M = 2$ Eigenfunction 17

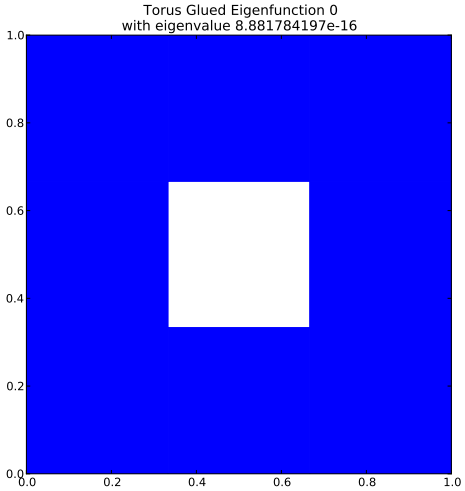
$M = 2$ Eigenfunction 17 has eigenvalue 2.53542968744





Compare to $m = 1$ eigenspace with eigenvalue 8.881784197e-16

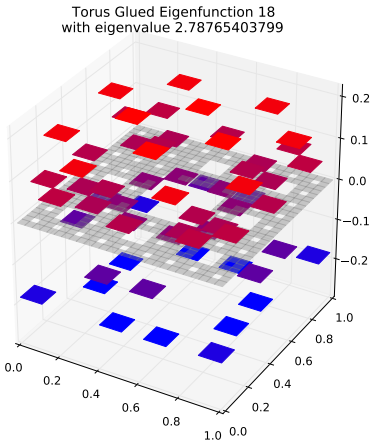


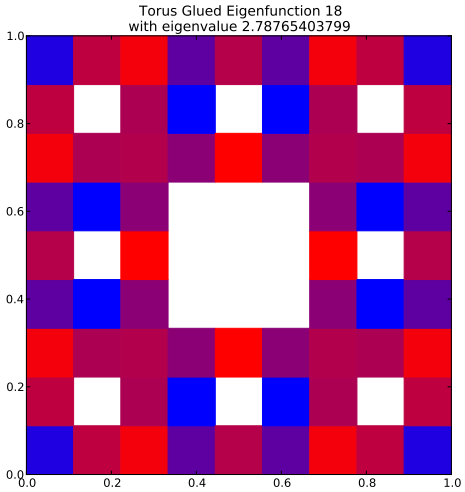


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 2.8546400489e + 15$
Dot Value: 2

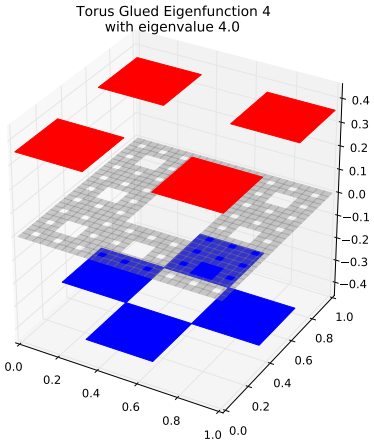
19 $M = 2$ Eigenfunction 18

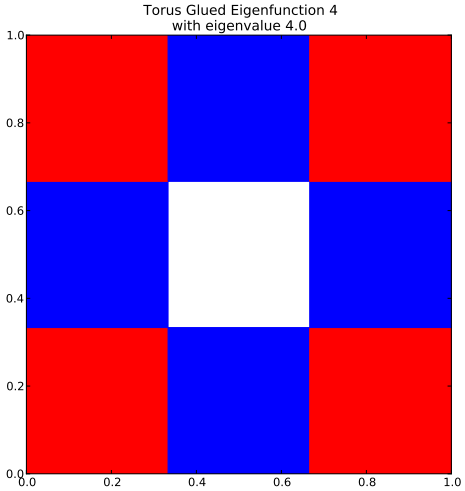
$M = 2$ Eigenfunction 18 has eigenvalue 2.78765403799





Compare to $m = 1$ eigenspace with eigenvalue 4.0

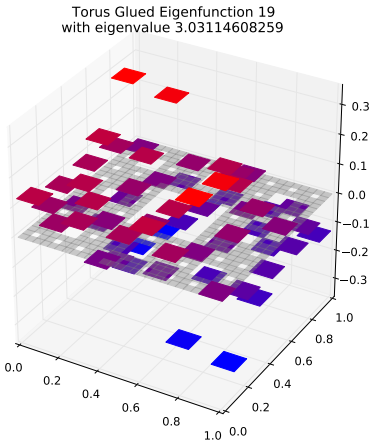


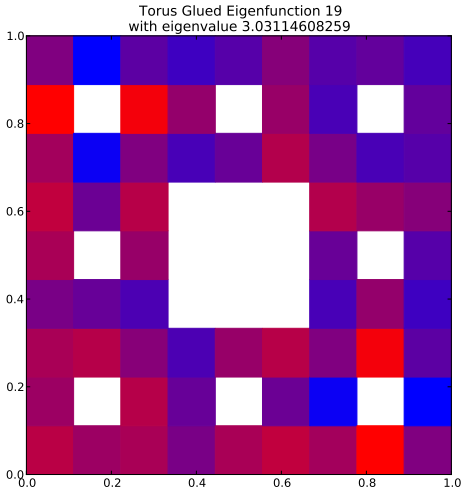


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 0.696913509497$
Dot Value: 0.0

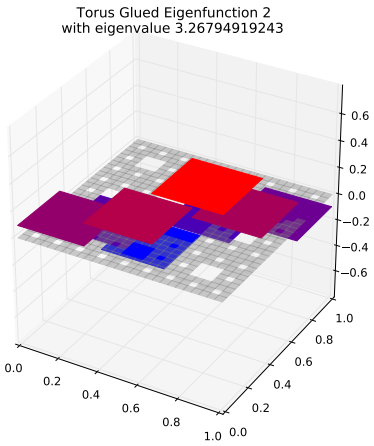
20 $M = 2$ Eigenfunction 19

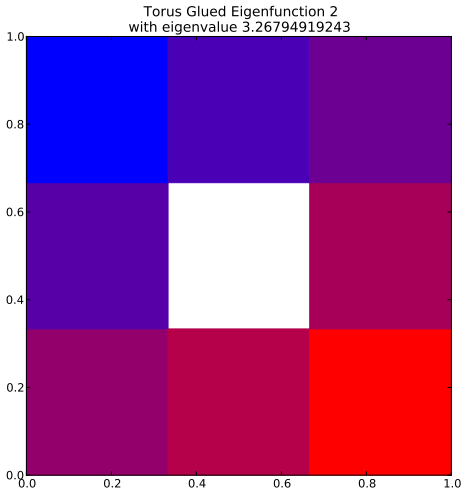
$M = 2$ Eigenfunction 19 has eigenvalue 3.03114608259





Compare to $m = 1$ eigenspace with eigenvalue 3.26794919243
(Note: Eigenspace Dimension > 1)

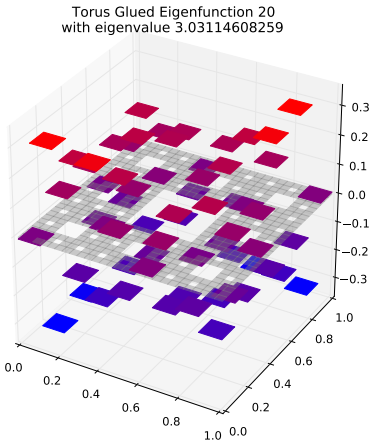


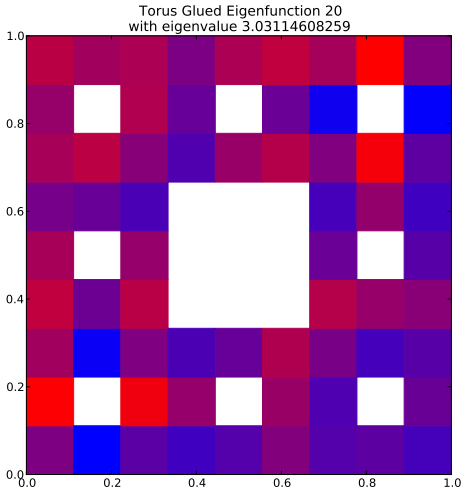


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 0.927537701507$
Dot Value: 0.007550097877229489

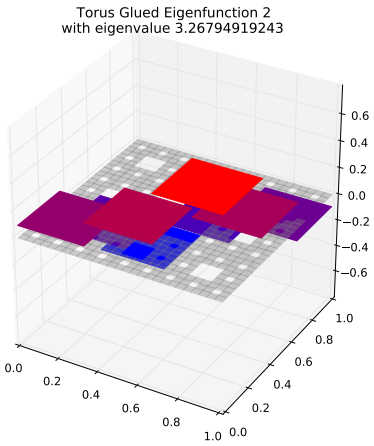
21 $M = 2$ Eigenfunction 20

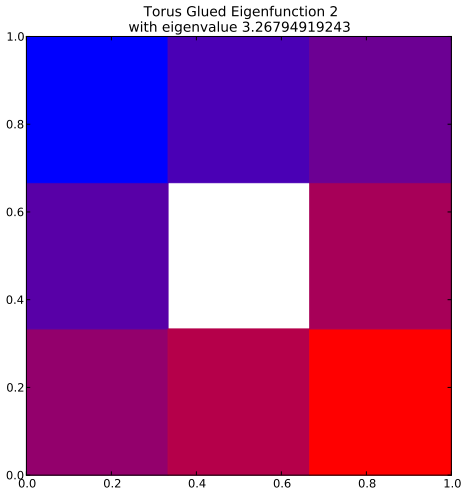
$M = 2$ Eigenfunction 20 has eigenvalue 3.03114608259





Compare to $m = 1$ eigenspace with eigenvalue 3.26794919243
(Note: Eigenspace Dimension > 1)

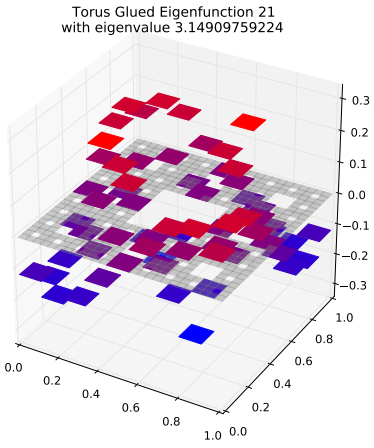


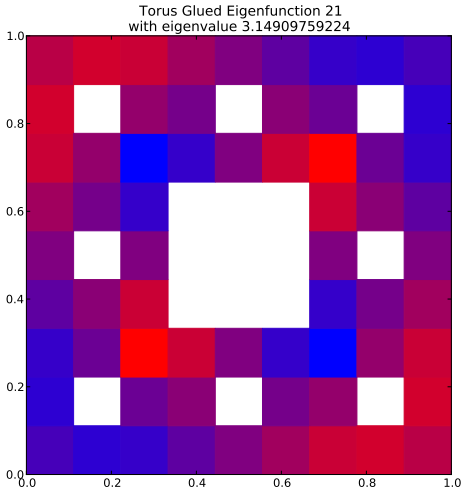


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 0.927537701507$
Dot Value: 0.007550097877230488

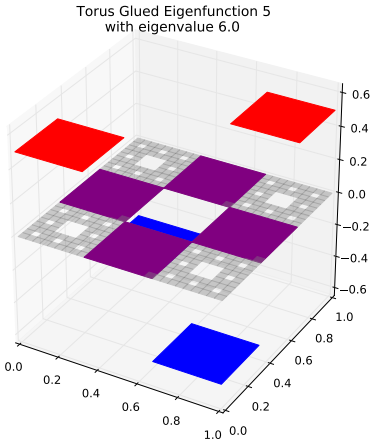
22 $M = 2$ Eigenfunction 21

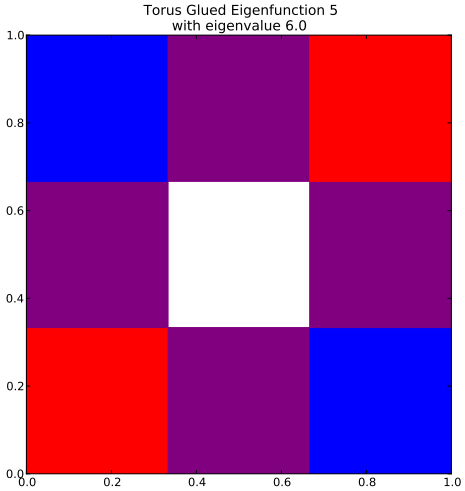
$M = 2$ Eigenfunction 21 has eigenvalue 3.14909759224





Compare to $m = 1$ eigenspace with eigenvalue 6.0

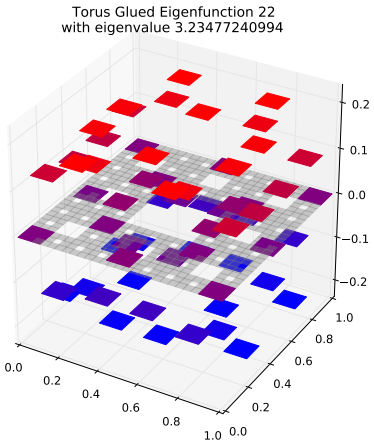


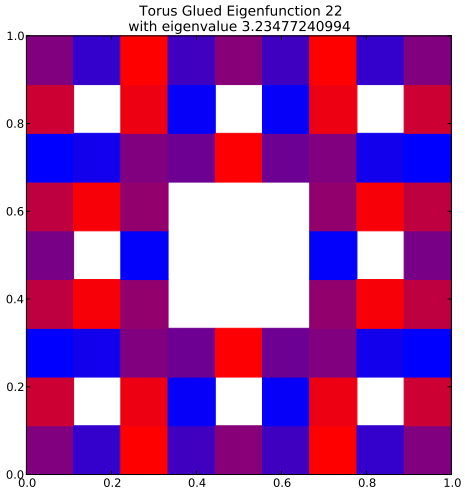


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 0.524849598707$
Dot Value: 0.0

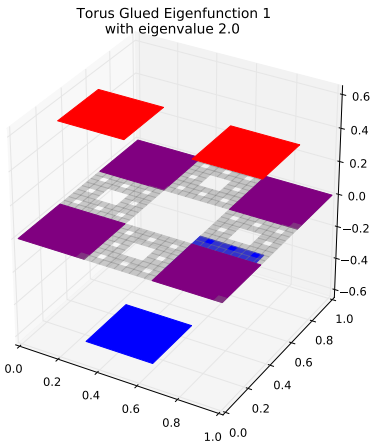
23 $M = 2$ Eigenfunction 22

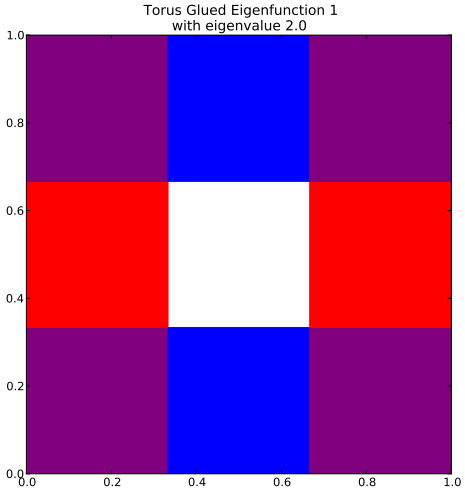
$M = 2$ Eigenfunction 22 has eigenvalue 3.23477240994





Compare to $m = 1$ eigenspace with eigenvalue 2.0

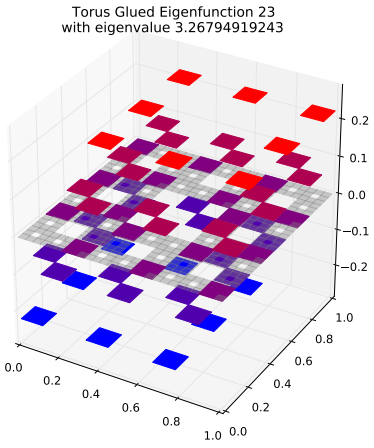


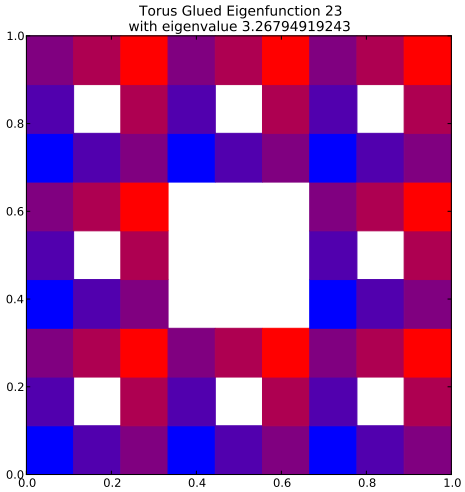


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 1.61738620497$
Dot Value: 0.0

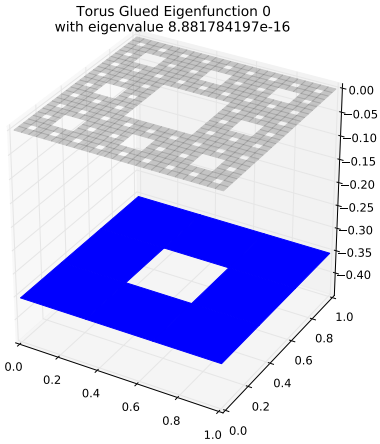
24 $M = 2$ Eigenfunction 23

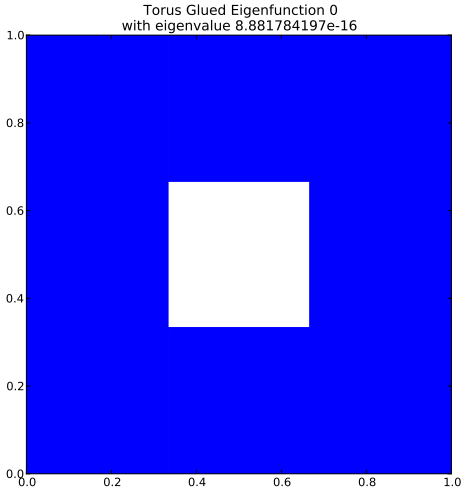
$M = 2$ Eigenfunction 23 has eigenvalue 3.26794919243





Compare to $m = 1$ eigenspace with eigenvalue 8.881784197e-16

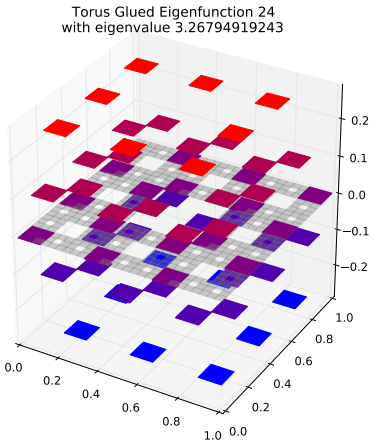


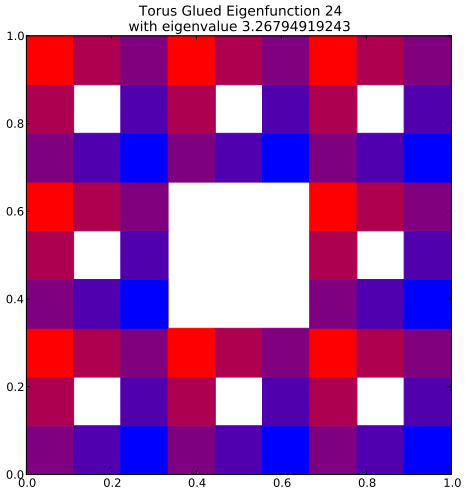


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 3.67938369132e + 15$
Dot Value: 2

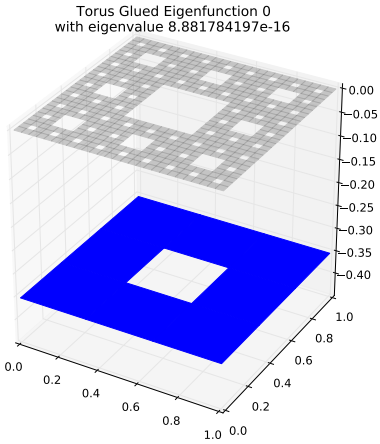
25 $M = 2$ Eigenfunction 24

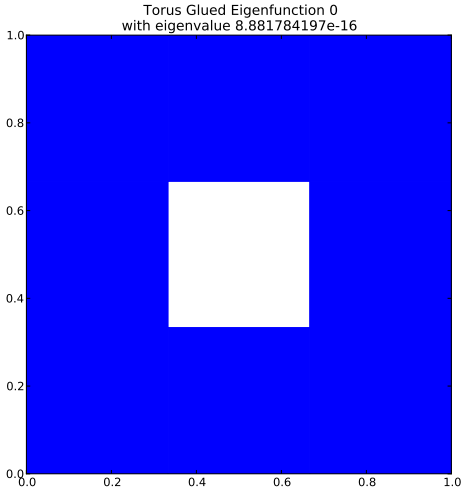
$M = 2$ Eigenfunction 24 has eigenvalue 3.26794919243





Compare to $m = 1$ eigenspace with eigenvalue 8.881784197e-16

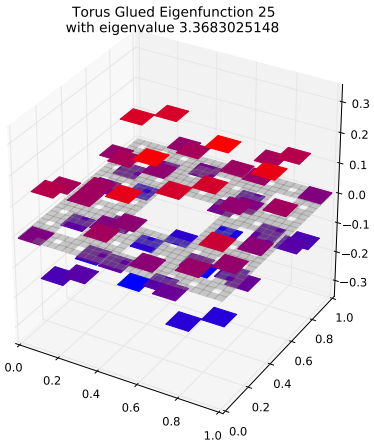


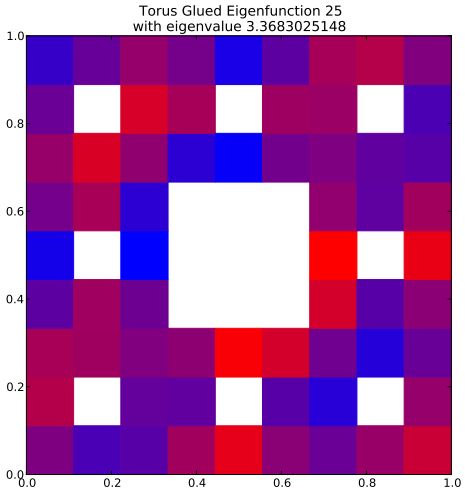


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 3.67938369132e + 15$
Dot Value: 2

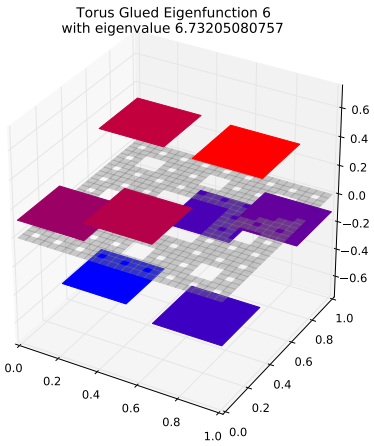
26 $M = 2$ Eigenfunction 25

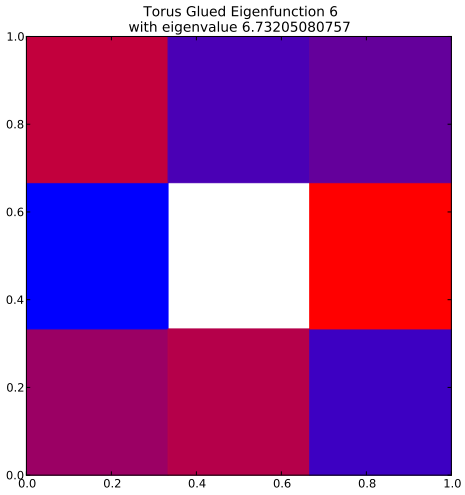
$M = 2$ Eigenfunction 25 has eigenvalue 3.3683025148





Compare to $m = 1$ eigenspace with eigenvalue 6.73205080757
(Note: Eigenspace Dimension > 1)

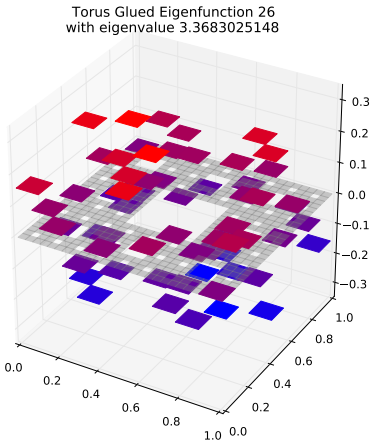


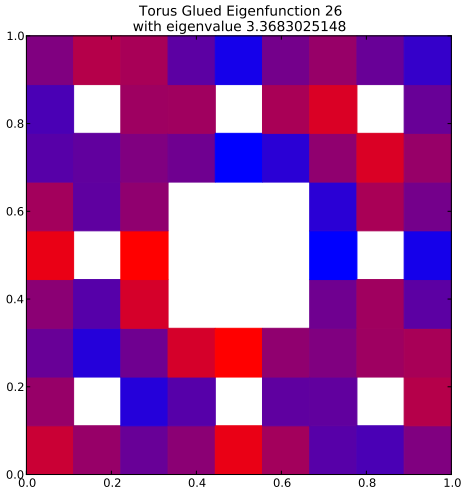


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 0.500338249232$
Dot Value: 0.02112597089916579

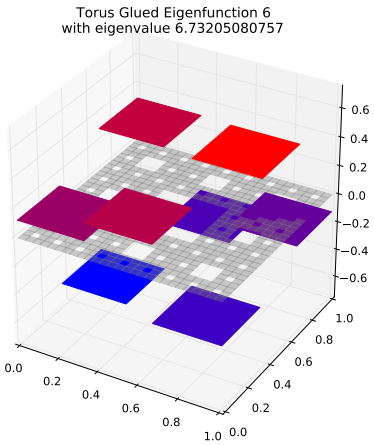
27 $M = 2$ Eigenfunction 26

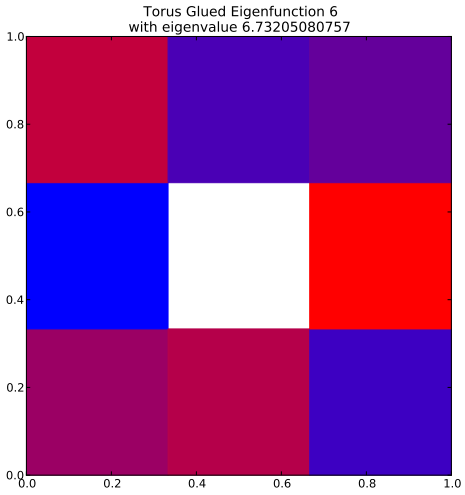
$M = 2$ Eigenfunction 26 has eigenvalue 3.3683025148





Compare to $m = 1$ eigenspace with eigenvalue 6.73205080757
(Note: Eigenspace Dimension > 1)

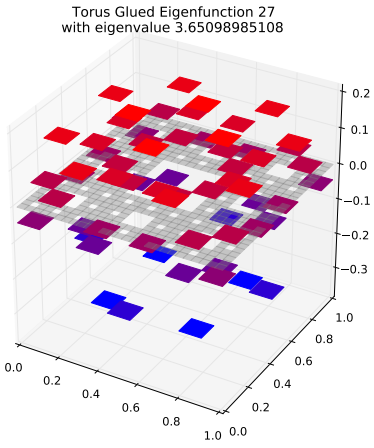


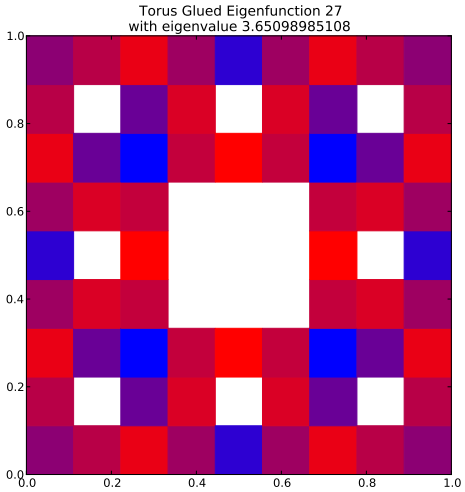


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 0.500338249232$
Dot Value: 0.021125970899165347

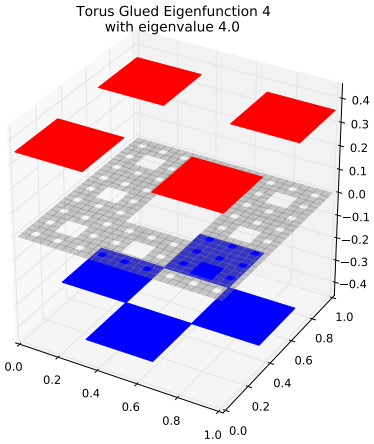
28 $M = 2$ Eigenfunction 27

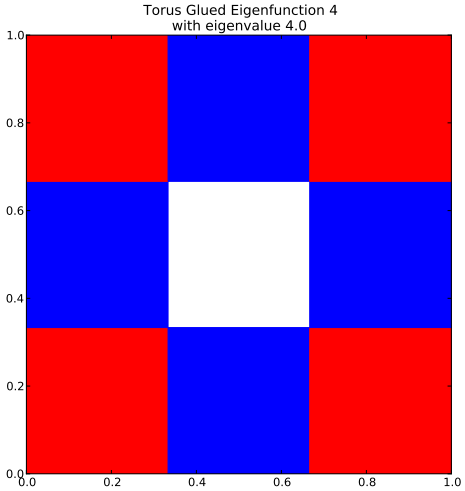
$M = 2$ Eigenfunction 27 has eigenvalue 3.65098985108





Compare to $m = 1$ eigenspace with eigenvalue 4.0

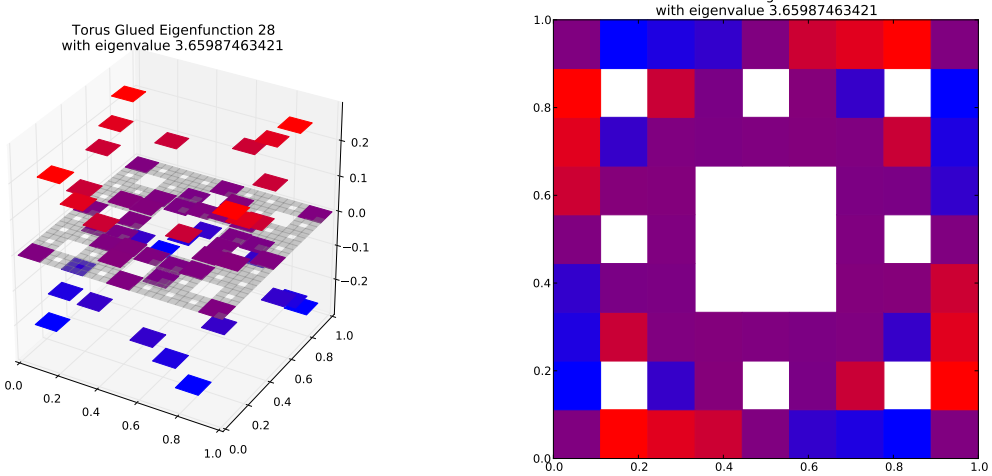




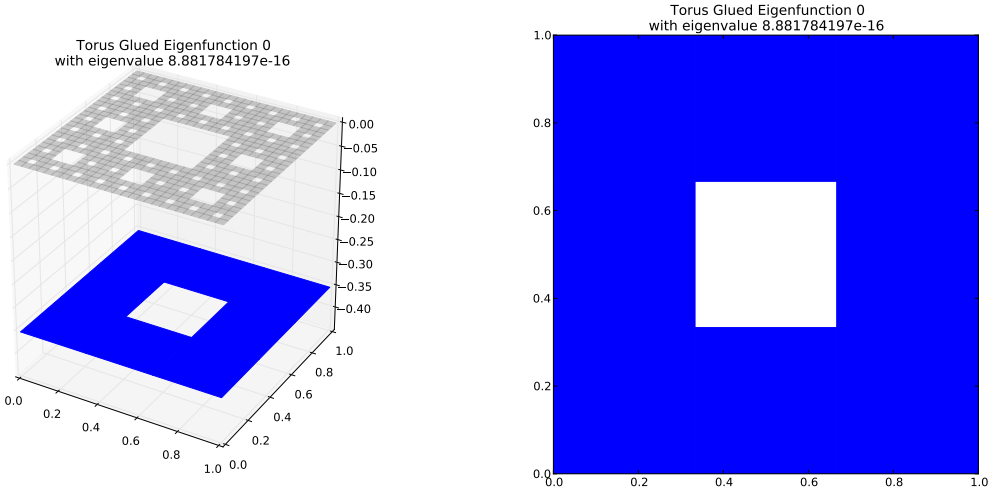
Eigenvalue Ratio: $\lambda_2/\lambda_1 = 0.912747462769$
Dot Value: 0.0

29 $M = 2$ Eigenfunction 28

$M = 2$ Eigenfunction 28 has eigenvalue 3.65987463421



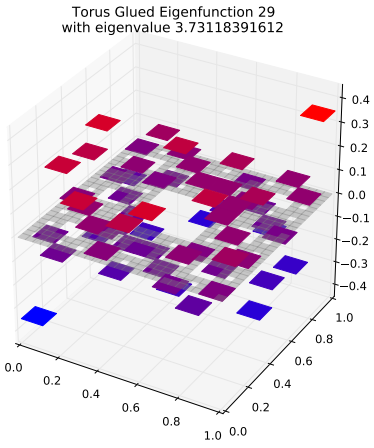
Compare to $m = 1$ eigenspace with eigenvalue 8.881784197e-16

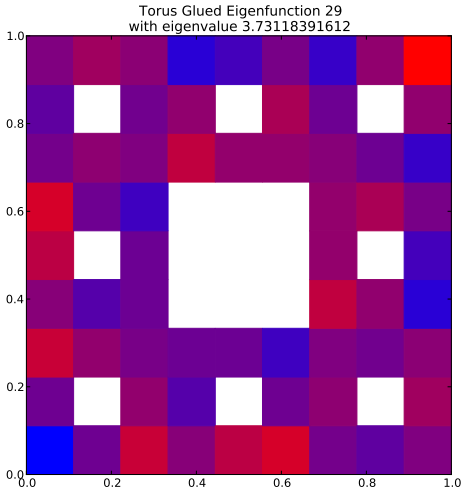


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 4.12065250972e + 15$
Dot Value: 2

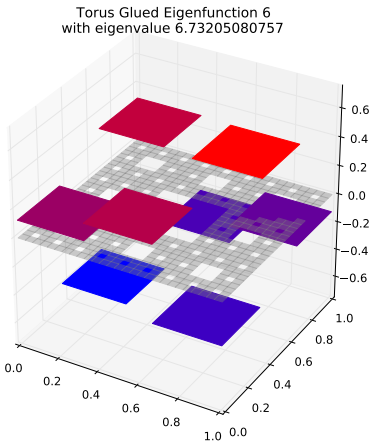
30 $M = 2$ Eigenfunction 29

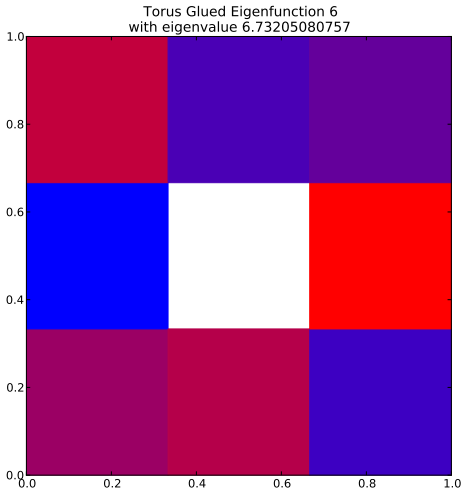
$M = 2$ Eigenfunction 29 has eigenvalue 3.73118391612





Compare to $m = 1$ eigenspace with eigenvalue 6.73205080757
(Note: Eigenspace Dimension > 1)

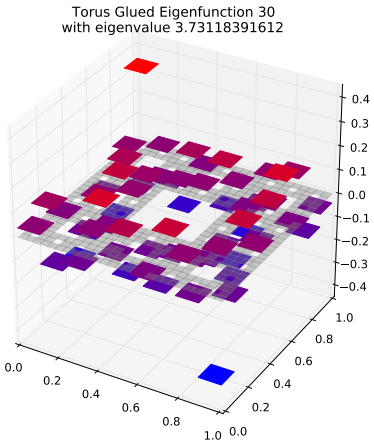


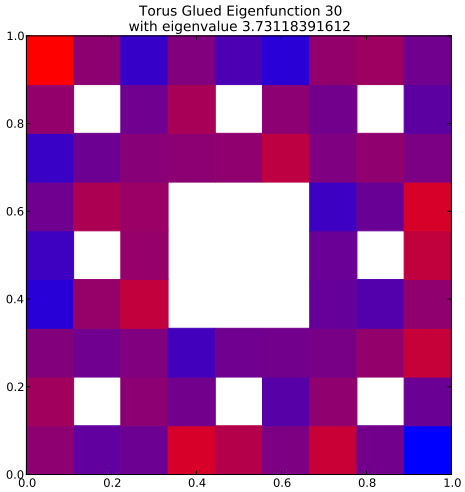


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 0.554241793886$
Dot Value: 0.028736508594888743

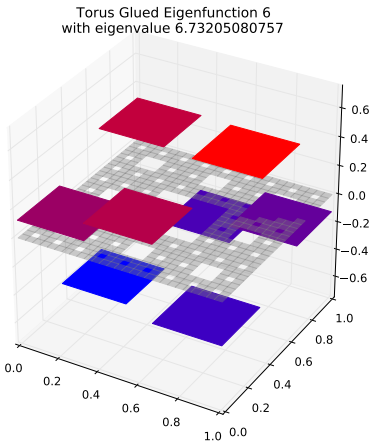
31 $M = 2$ Eigenfunction 30

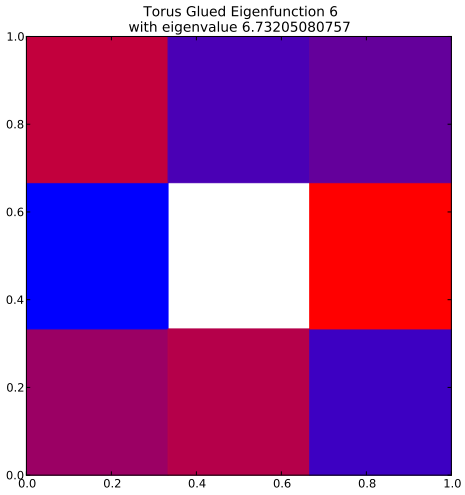
$M = 2$ Eigenfunction 30 has eigenvalue 3.73118391612





Compare to $m = 1$ eigenspace with eigenvalue 6.73205080757
(Note: Eigenspace Dimension > 1)

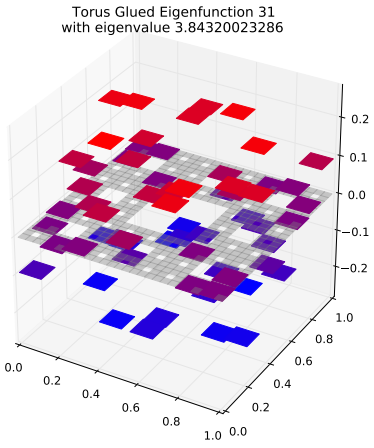


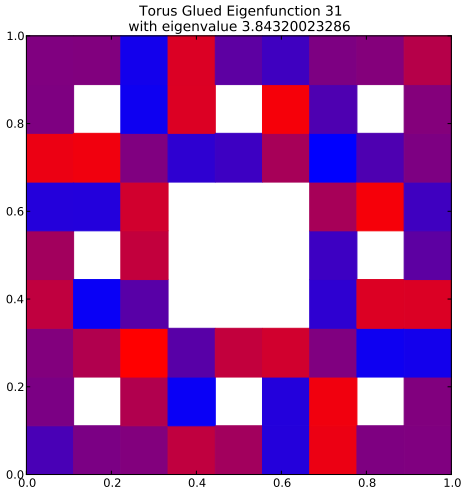


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 0.554241793886$
Dot Value: 0.02873650859488397

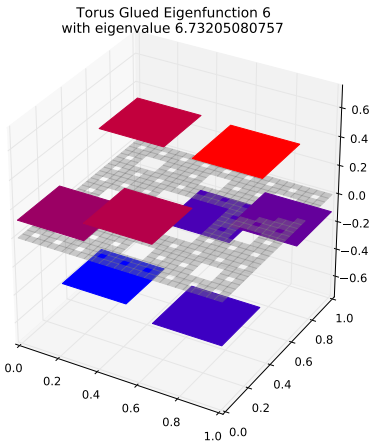
32 $M = 2$ Eigenfunction 31

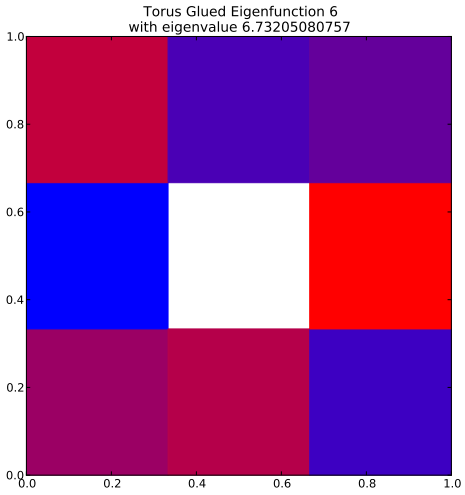
$M = 2$ Eigenfunction 31 has eigenvalue 3.84320023286





Compare to $m = 1$ eigenspace with eigenvalue 6.73205080757
(Note: Eigenspace Dimension > 1)

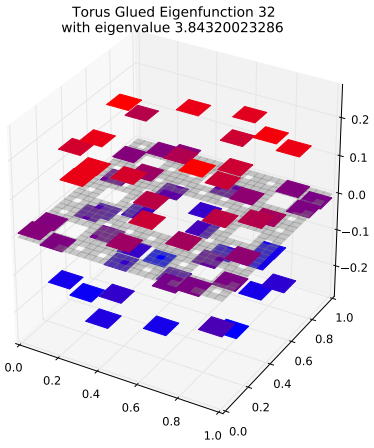


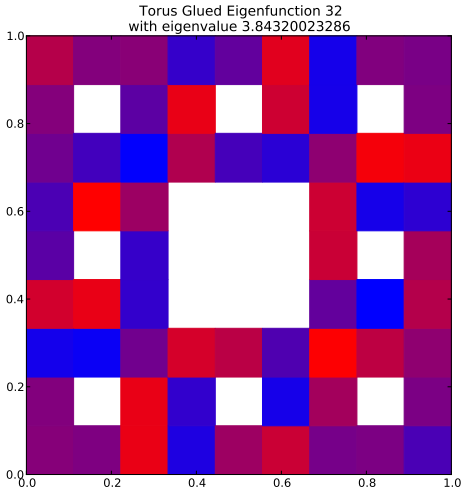


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 0.570881049878$
Dot Value: 0.08754815732229404

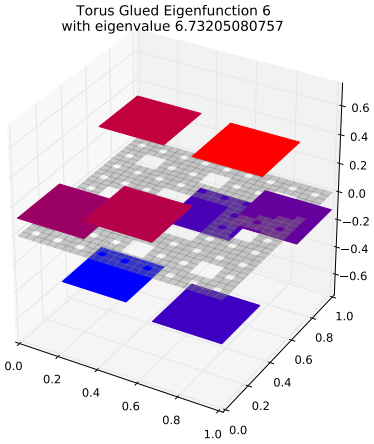
33 $M = 2$ Eigenfunction 32

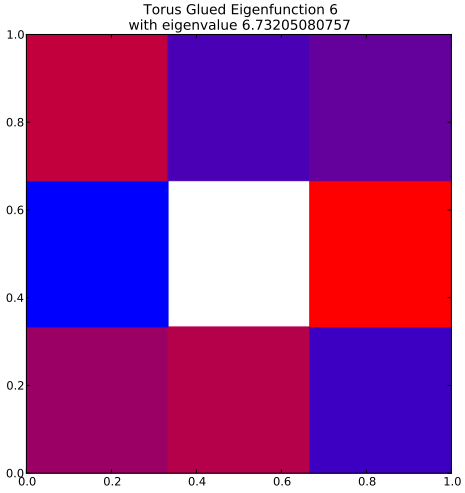
$M = 2$ Eigenfunction 32 has eigenvalue 3.84320023286





Compare to $m = 1$ eigenspace with eigenvalue 6.73205080757
(Note: Eigenspace Dimension > 1)

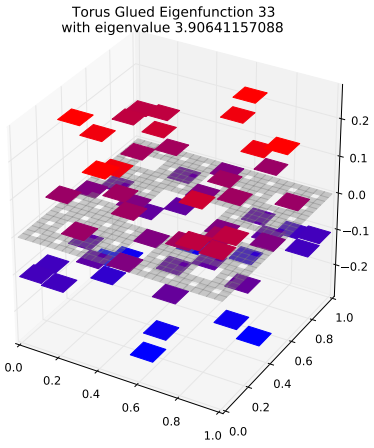


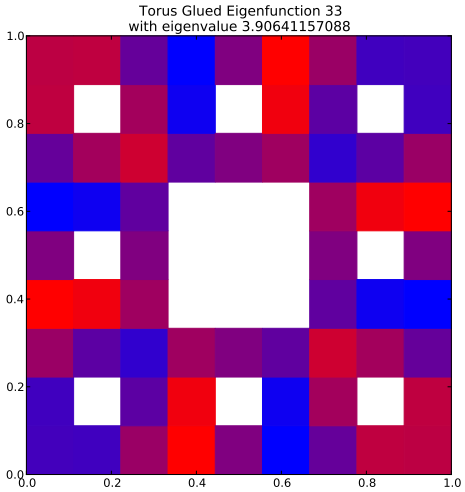


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 0.570881049878$
Dot Value: 0.08754815732229271

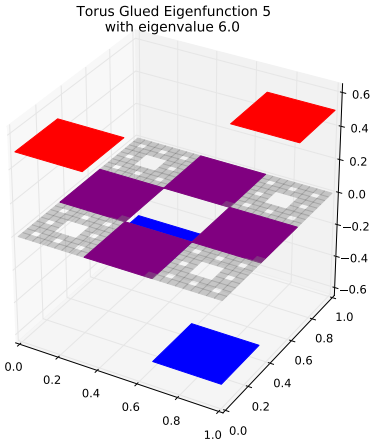
34 $M = 2$ Eigenfunction 33

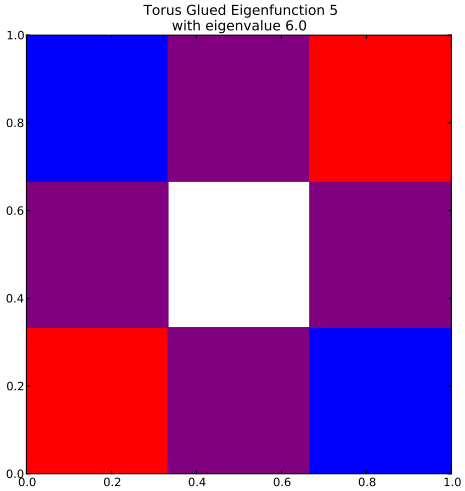
$M = 2$ Eigenfunction 33 has eigenvalue 3.90641157088





Compare to $m = 1$ eigenspace with eigenvalue 6.0

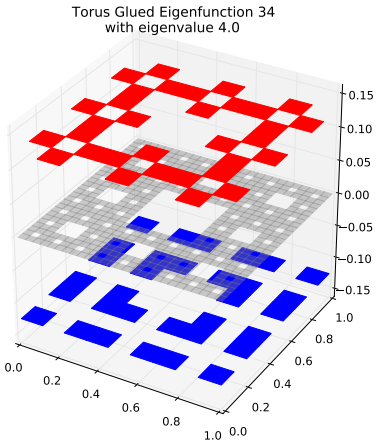


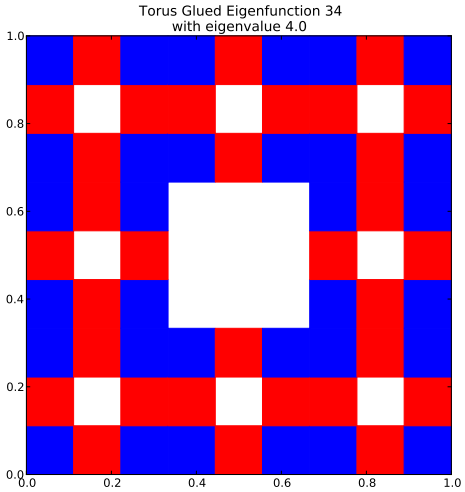


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 0.651068595146$
Dot Value: 0.0

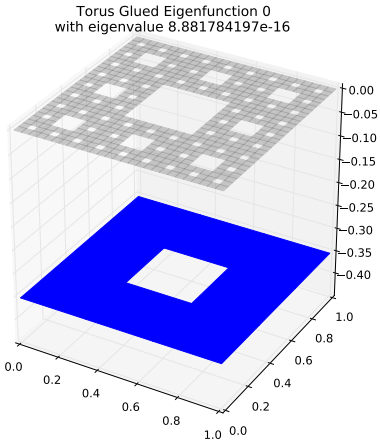
35 $M = 2$ Eigenfunction 34

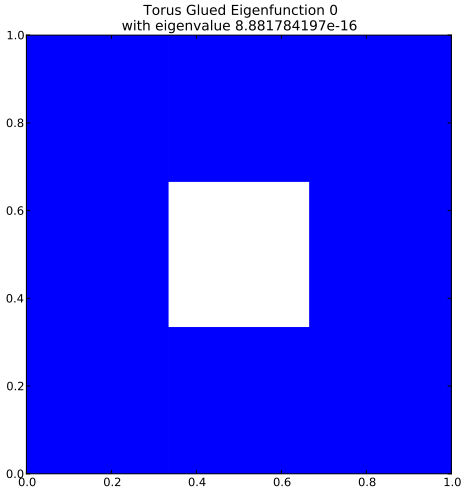
$M = 2$ Eigenfunction 34 has eigenvalue 4.0





Compare to $m = 1$ eigenspace with eigenvalue 8.881784197e-16

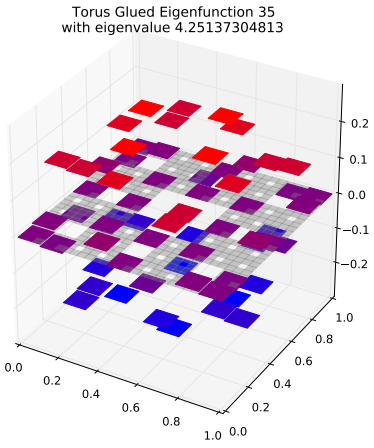


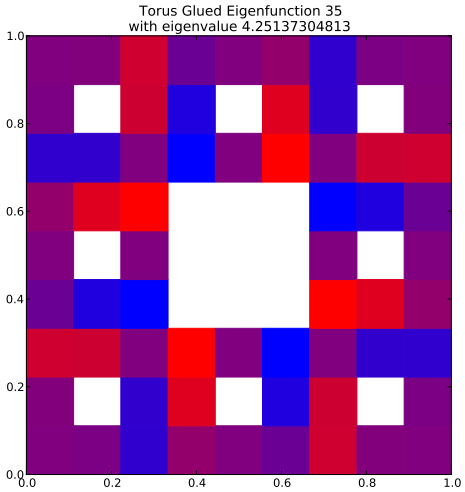


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 4.50359962737e + 15$
Dot Value: 2

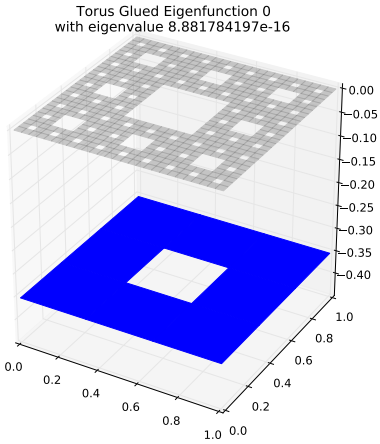
36 $M = 2$ Eigenfunction 35

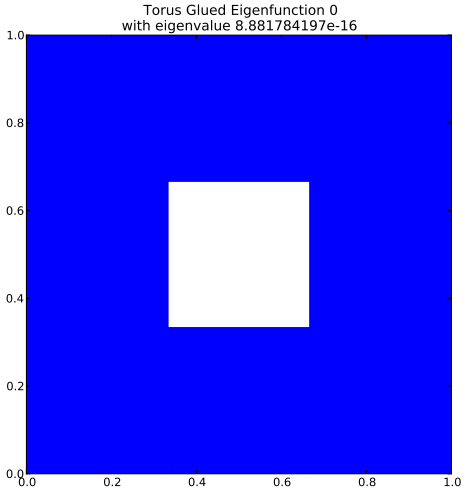
$M = 2$ Eigenfunction 35 has eigenvalue 4.25137304813





Compare to $m = 1$ eigenspace with eigenvalue 8.881784197e-16

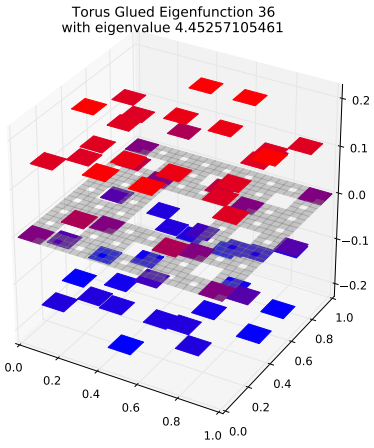


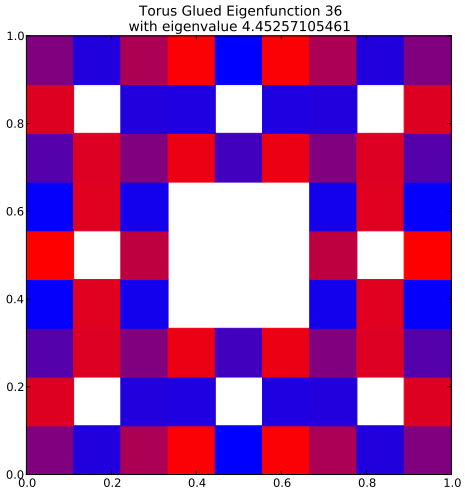


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 4.78662051884e + 15$
Dot Value: 2

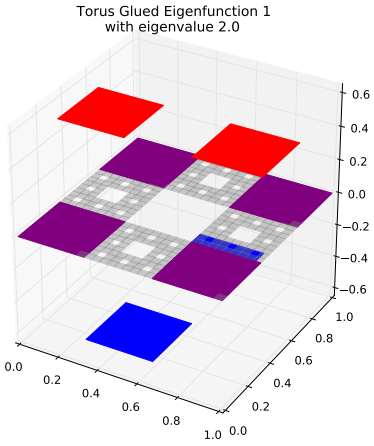
37 $M = 2$ Eigenfunction 36

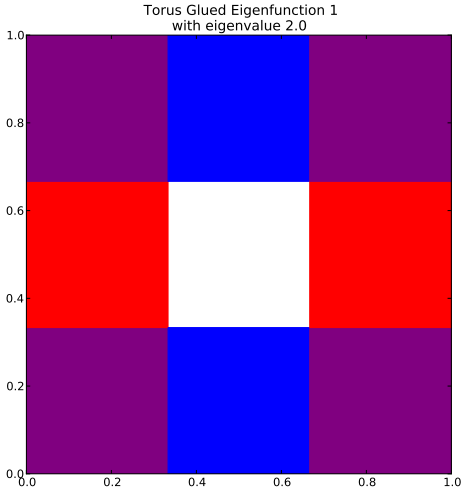
$M = 2$ Eigenfunction 36 has eigenvalue 4.45257105461





Compare to $m = 1$ eigenspace with eigenvalue 2.0

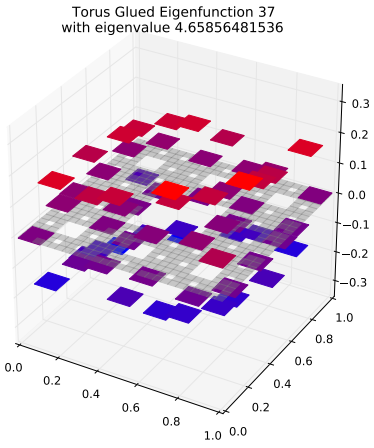


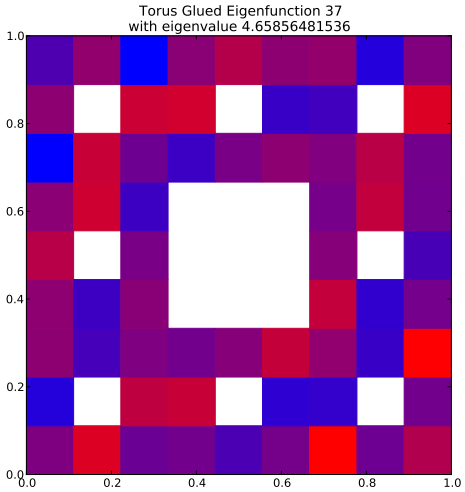


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 2.2262855273$
Dot Value: 0.0

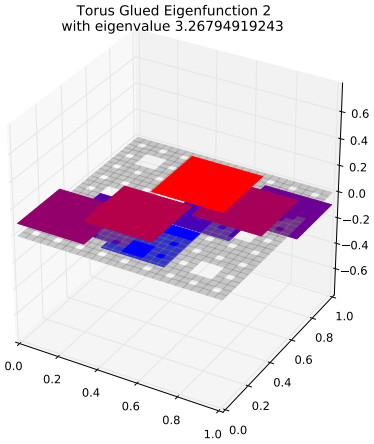
38 $M = 2$ Eigenfunction 37

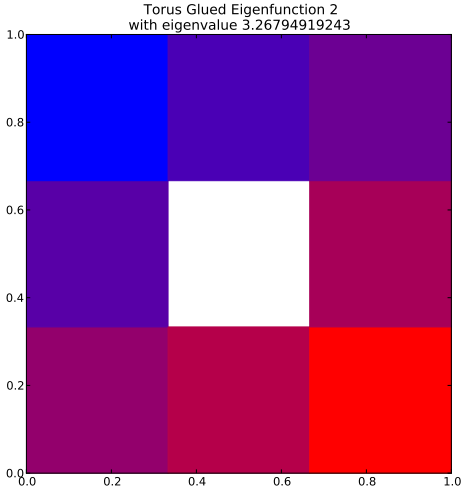
$M = 2$ Eigenfunction 37 has eigenvalue 4.65856481536





Compare to $m = 1$ eigenspace with eigenvalue 3.26794919243
(Note: Eigenspace Dimension > 1)

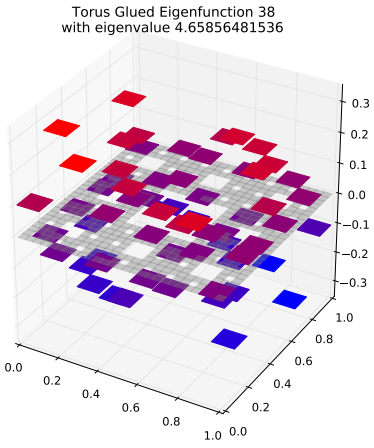


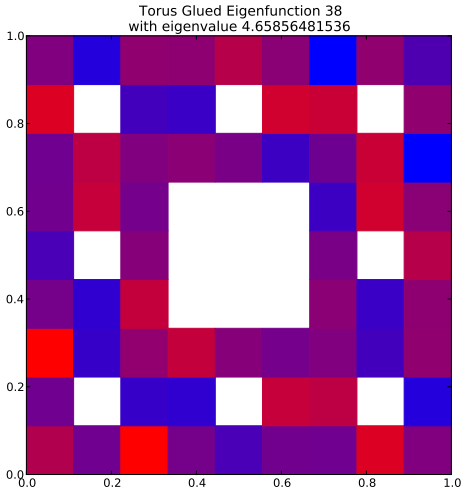


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 1.42553159215$
Dot Value: 0.26332463973073283

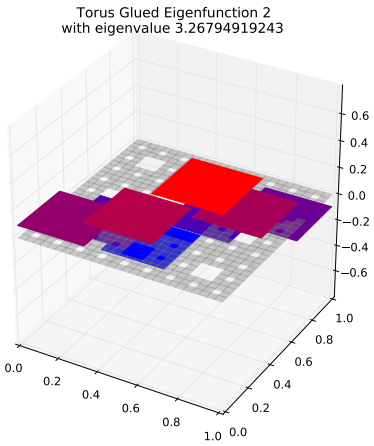
39 $M = 2$ Eigenfunction 38

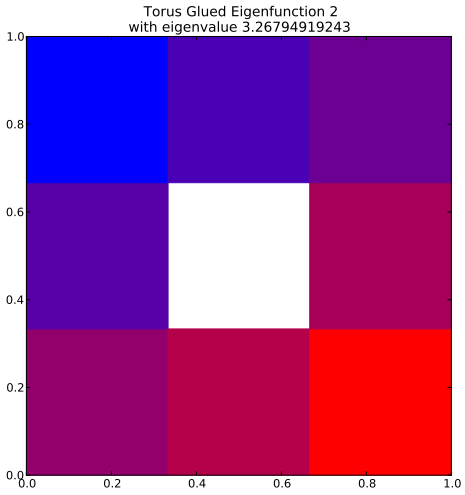
$M = 2$ Eigenfunction 38 has eigenvalue 4.65856481536





Compare to $m = 1$ eigenspace with eigenvalue 3.26794919243
(Note: Eigenspace Dimension > 1)

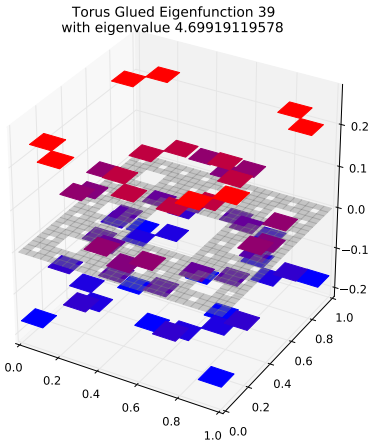


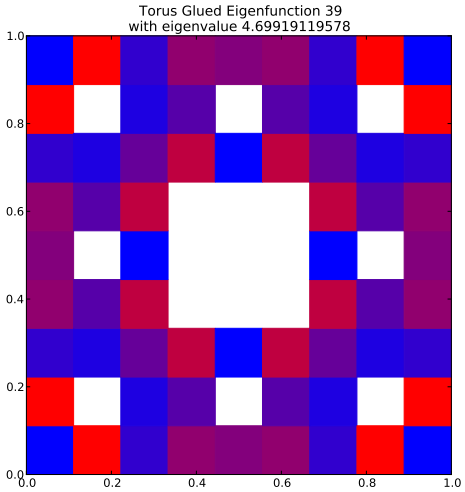


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 1.42553159215$
Dot Value: 0.26332463973073483

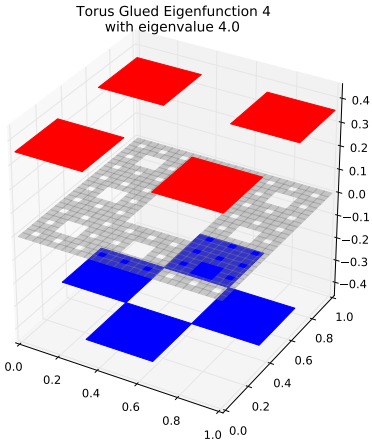
40 $M = 2$ Eigenfunction 39

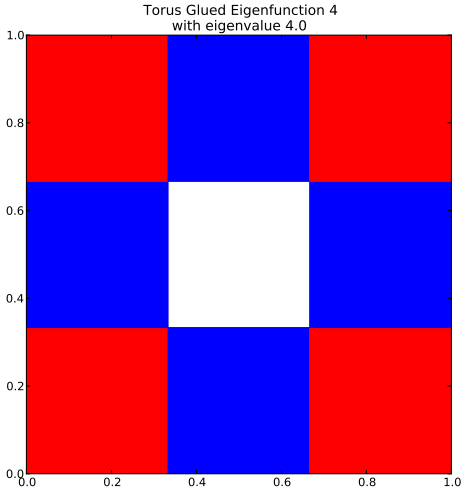
$M = 2$ Eigenfunction 39 has eigenvalue 4.69919119578





Compare to $m = 1$ eigenspace with eigenvalue 4.0

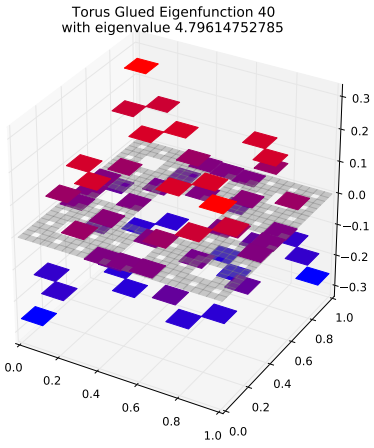


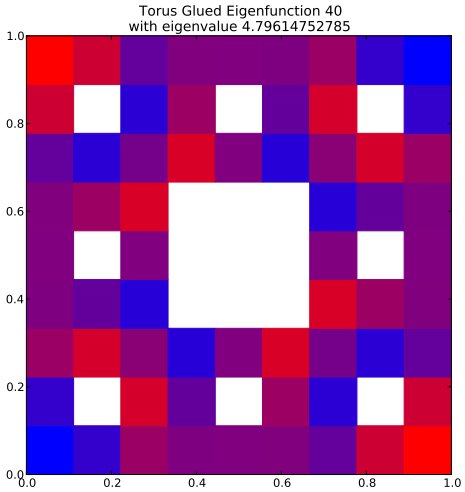


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 1.17479779895$
Dot Value: 0.0

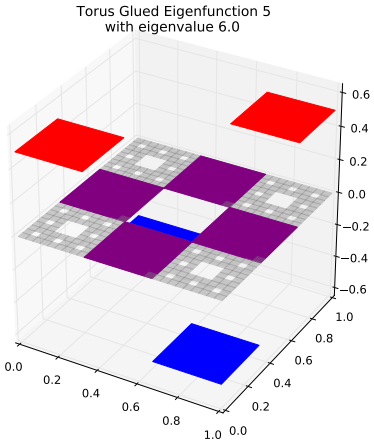
41 $M = 2$ Eigenfunction 40

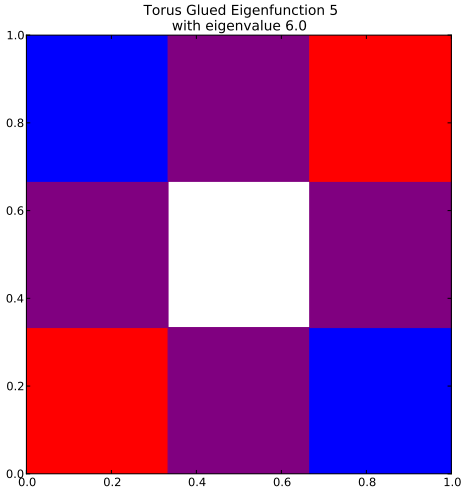
$M = 2$ Eigenfunction 40 has eigenvalue 4.79614752785





Compare to $m = 1$ eigenspace with eigenvalue 6.0

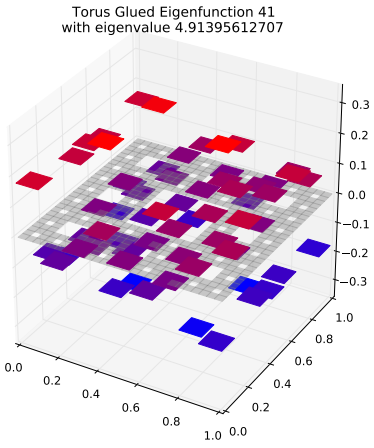


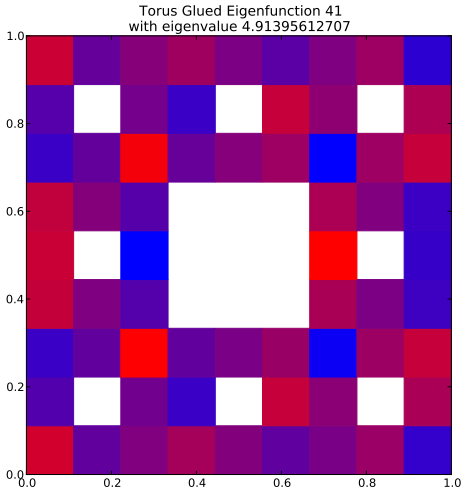


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 0.799357921309$
Dot Value: 2.220446049250313e-16

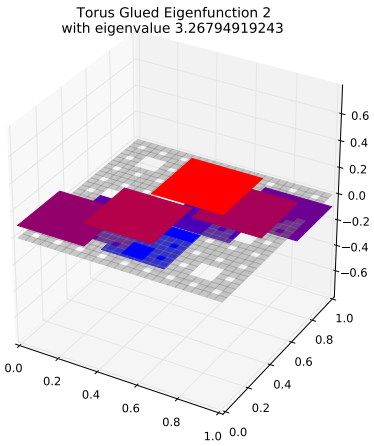
42 $M = 2$ Eigenfunction 41

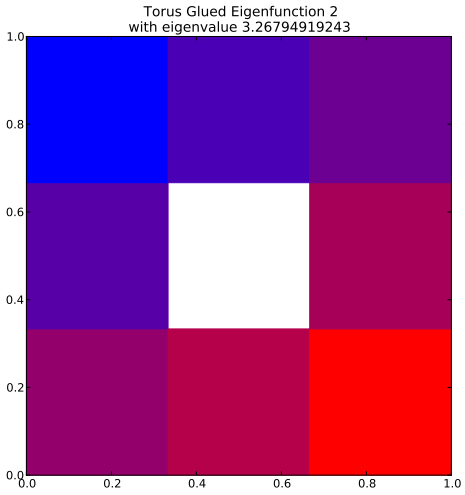
$M = 2$ Eigenfunction 41 has eigenvalue 4.91395612707





Compare to $m = 1$ eigenspace with eigenvalue 3.26794919243
(Note: Eigenspace Dimension > 1)

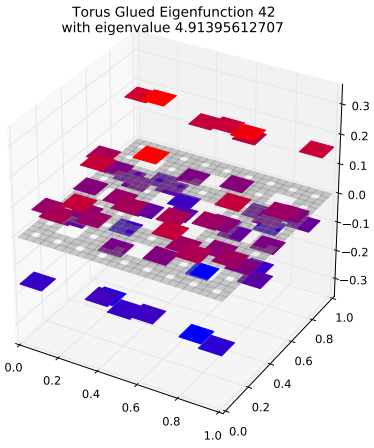


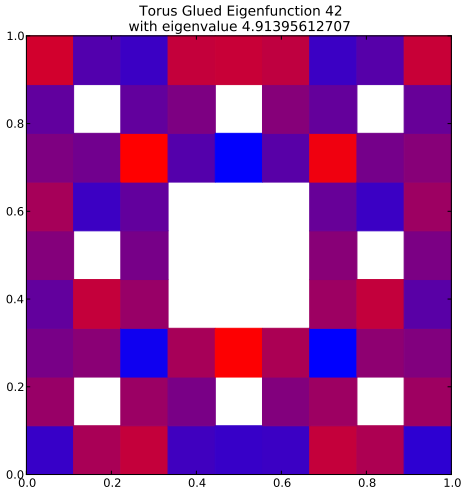


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 1.50368192335$
Dot Value: 0.11919793065129936

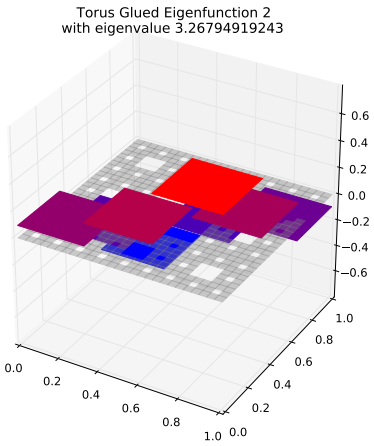
43 $M = 2$ Eigenfunction 42

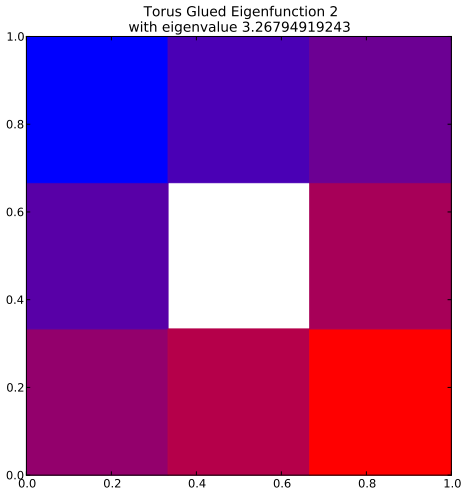
$M = 2$ Eigenfunction 42 has eigenvalue 4.91395612707





Compare to $m = 1$ eigenspace with eigenvalue 3.26794919243
(Note: Eigenspace Dimension > 1)

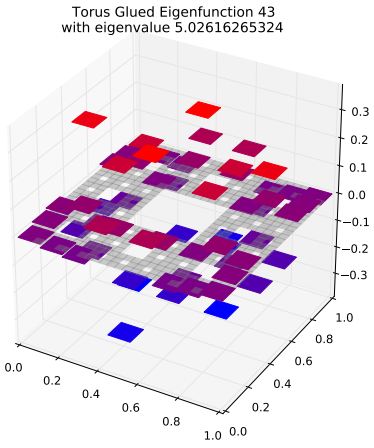


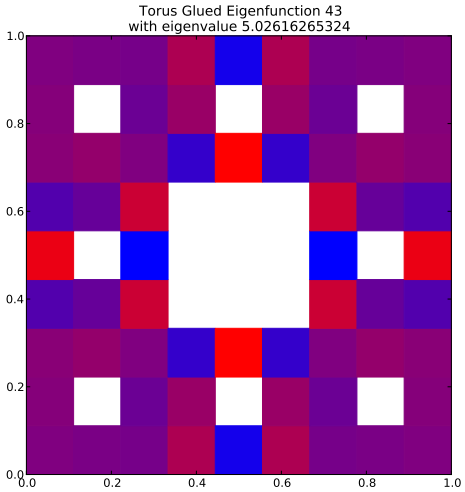


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 1.50368192335$
Dot Value: 0.11919793065128337

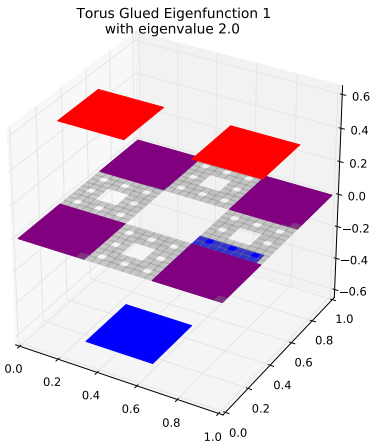
44 $M = 2$ Eigenfunction 43

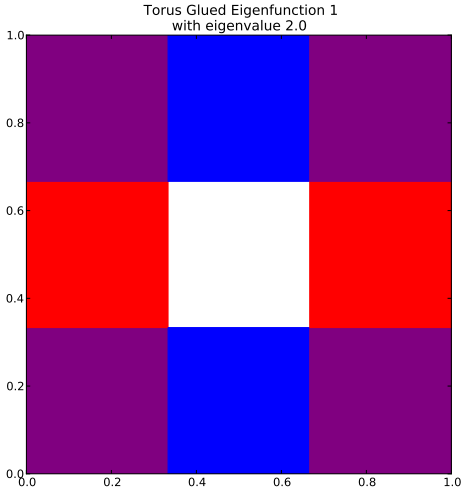
$M = 2$ Eigenfunction 43 has eigenvalue 5.02616265324





Compare to $m = 1$ eigenspace with eigenvalue 2.0

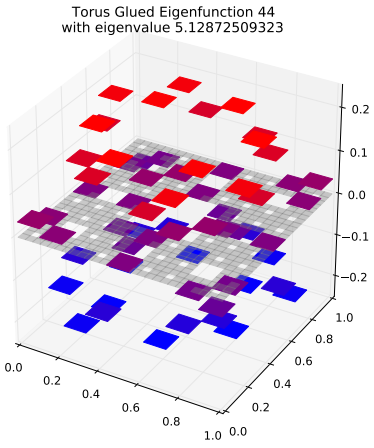


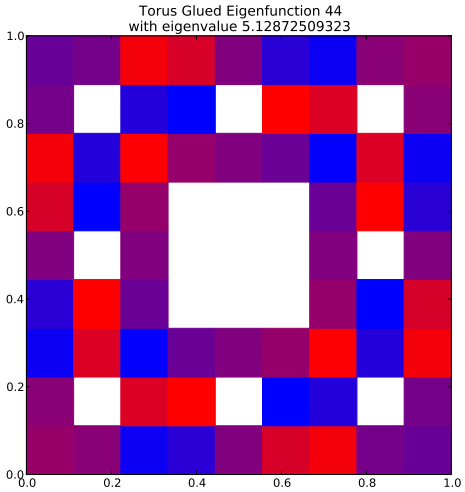


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 2.51308132662$
Dot Value: 0.0

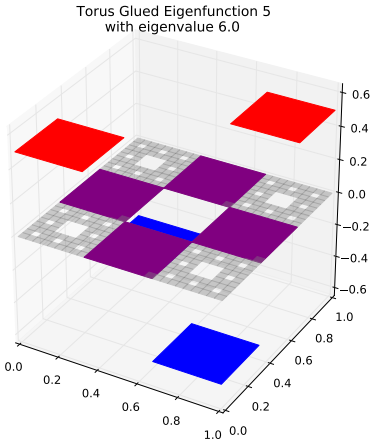
45 $M = 2$ Eigenfunction 44

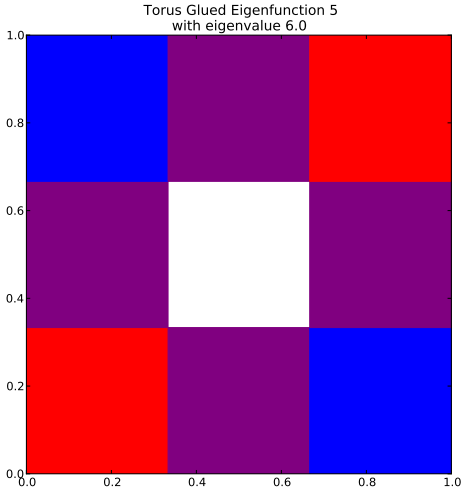
$M = 2$ Eigenfunction 44 has eigenvalue 5.12872509323





Compare to $m = 1$ eigenspace with eigenvalue 6.0

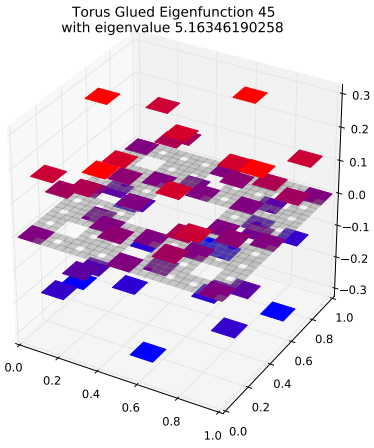


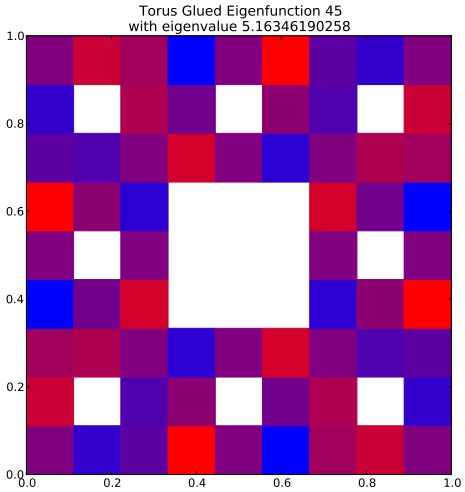


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 0.854787515539$
Dot Value: 0.0

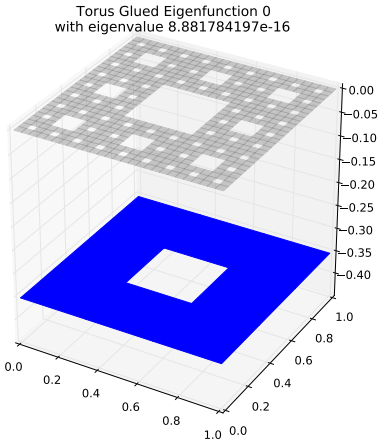
46 $M = 2$ Eigenfunction 45

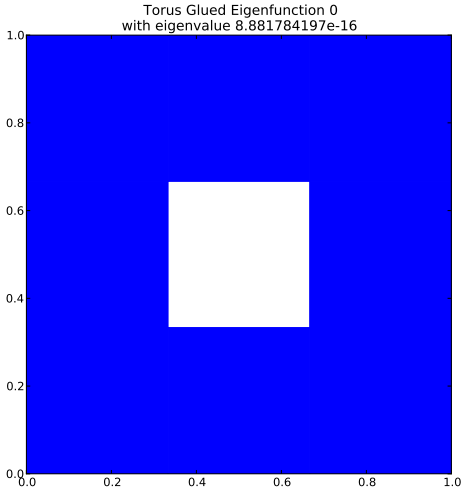
$M = 2$ Eigenfunction 45 has eigenvalue 5.16346190258





Compare to $m = 1$ eigenspace with eigenvalue 8.881784197e-16

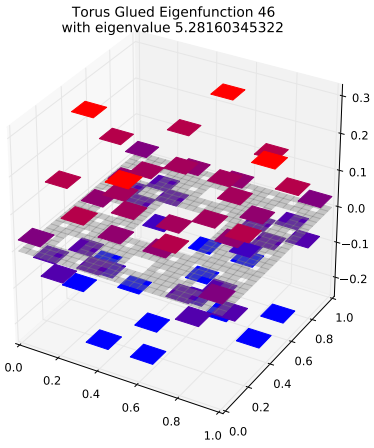


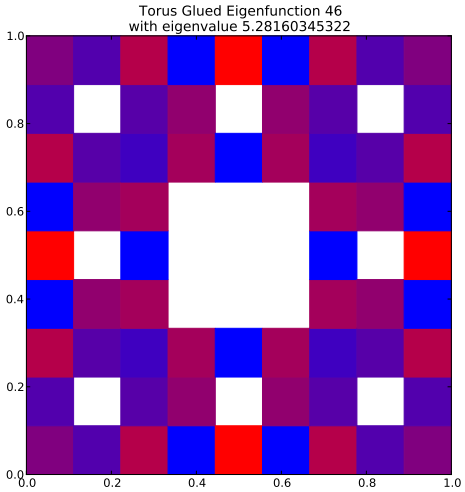


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 5.8135412751e + 15$
Dot Value: 2

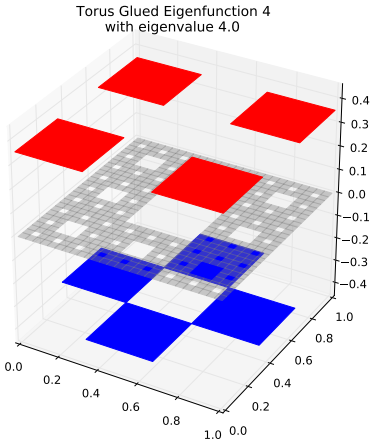
47 $M = 2$ Eigenfunction 46

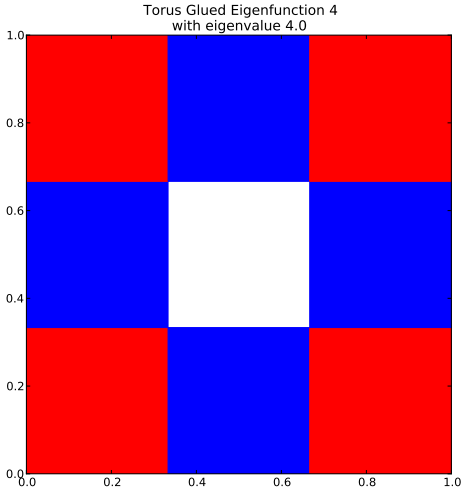
$M = 2$ Eigenfunction 46 has eigenvalue 5.28160345322





Compare to $m = 1$ eigenspace with eigenvalue 4.0

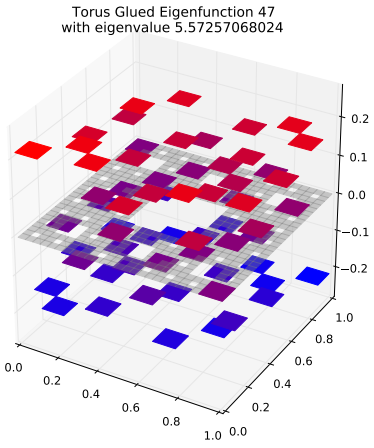


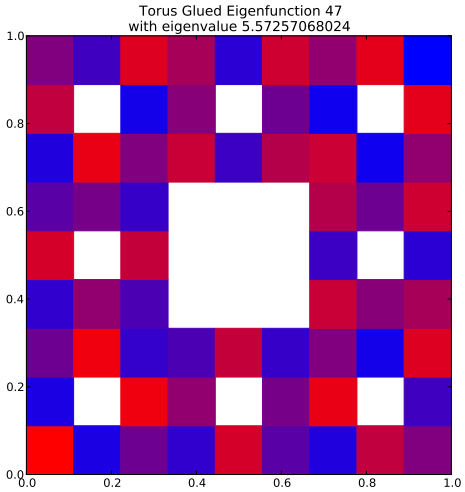


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 1.3204008633$
Dot Value: 0.0

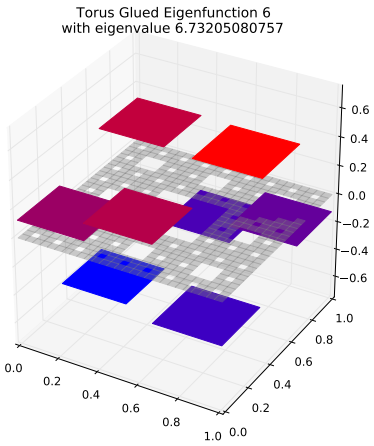
48 $M = 2$ Eigenfunction 47

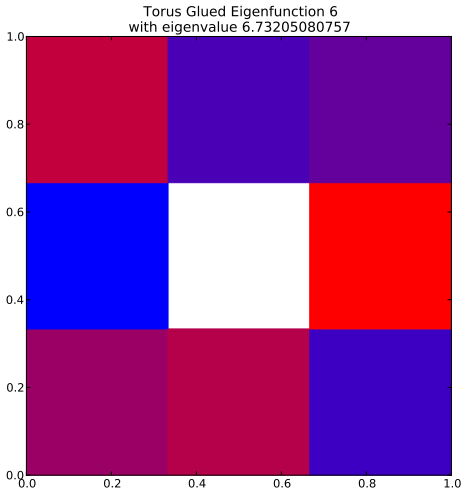
$M = 2$ Eigenfunction 47 has eigenvalue 5.57257068024





Compare to $m = 1$ eigenspace with eigenvalue 6.73205080757
(Note: Eigenspace Dimension > 1)

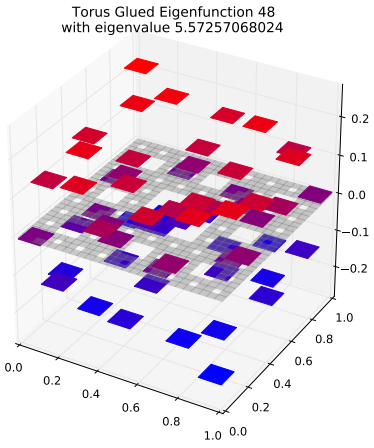


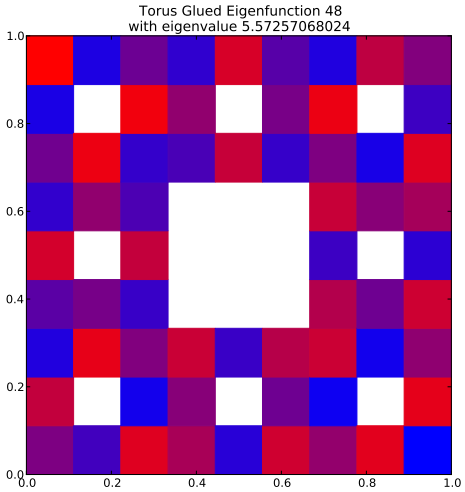


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 0.827767175194$
Dot Value: 0.008885431644714004

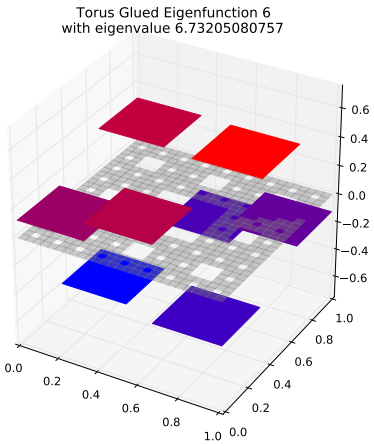
49 $M = 2$ Eigenfunction 48

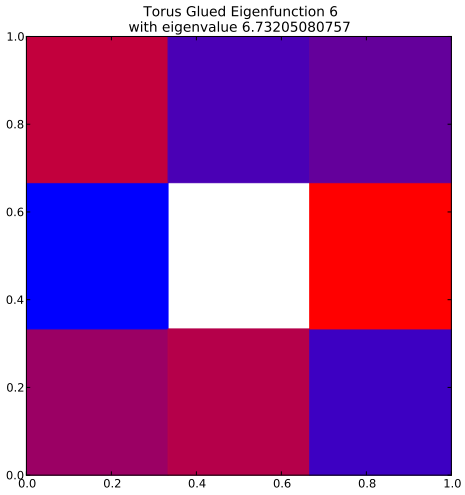
$M = 2$ Eigenfunction 48 has eigenvalue 5.57257068024





Compare to $m = 1$ eigenspace with eigenvalue 6.73205080757
(Note: Eigenspace Dimension > 1)

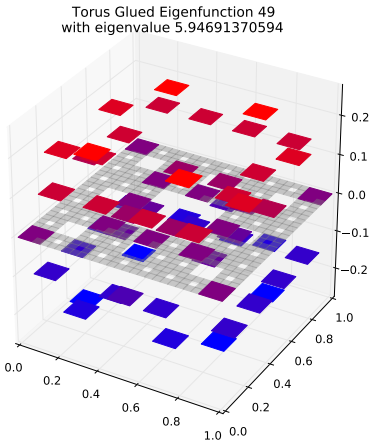


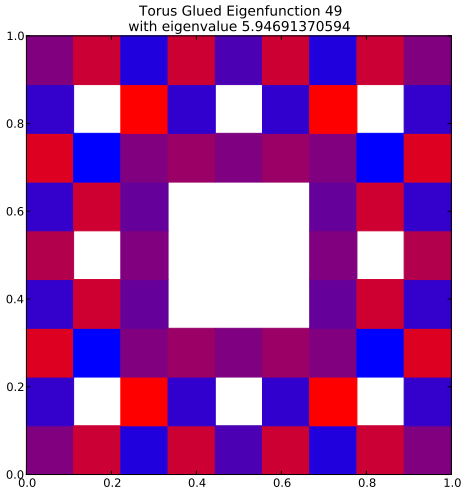


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 0.827767175194$
Dot Value: 0.008885431644713115

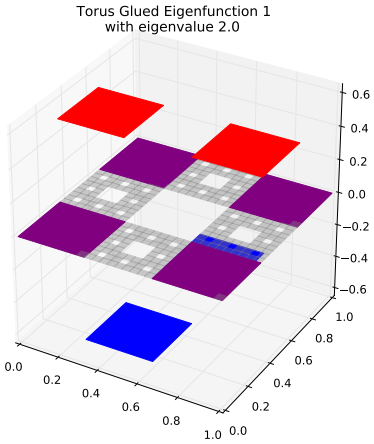
50 $M = 2$ Eigenfunction 49

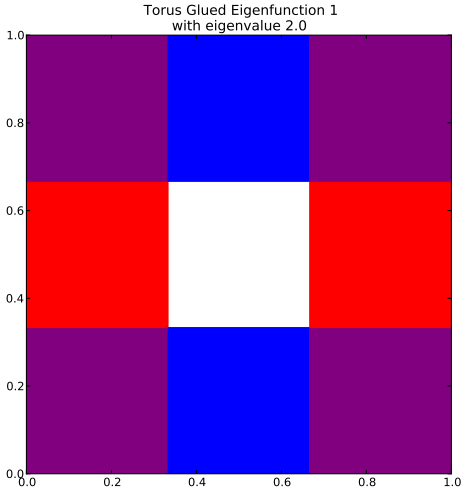
$M = 2$ Eigenfunction 49 has eigenvalue 5.94691370594





Compare to $m = 1$ eigenspace with eigenvalue 2.0

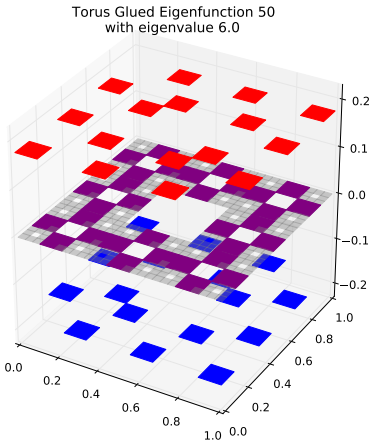


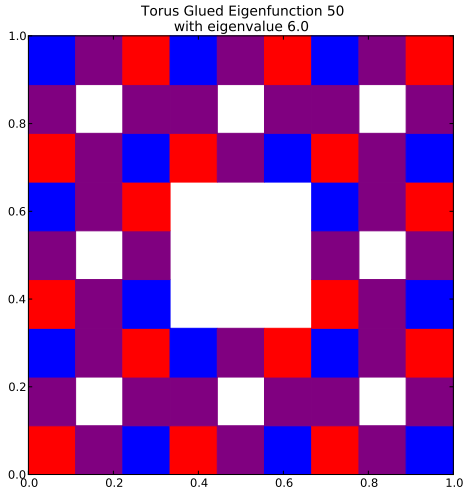


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 2.97345685297$
Dot Value: 0.0

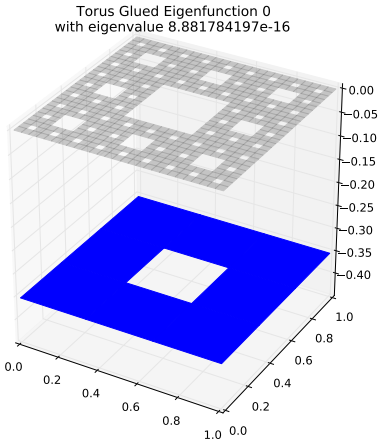
51 $M = 2$ Eigenfunction 50

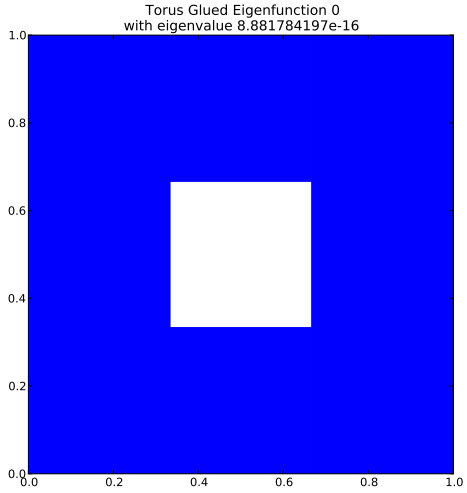
$M = 2$ Eigenfunction 50 has eigenvalue 6.0





Compare to $m = 1$ eigenspace with eigenvalue 8.881784197e-16

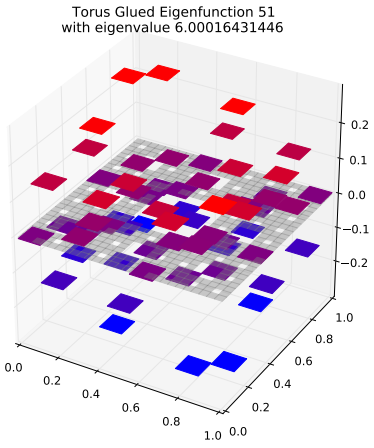


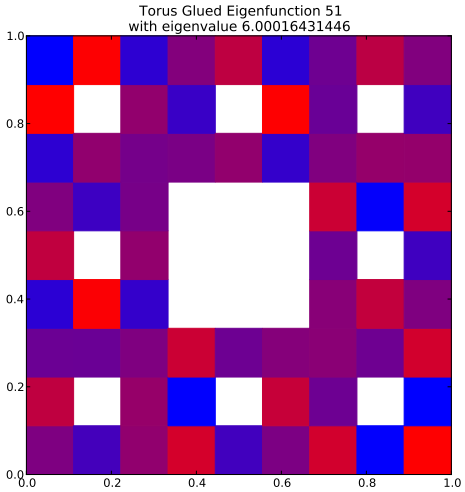


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 6.75539944106e + 15$
Dot Value: 2

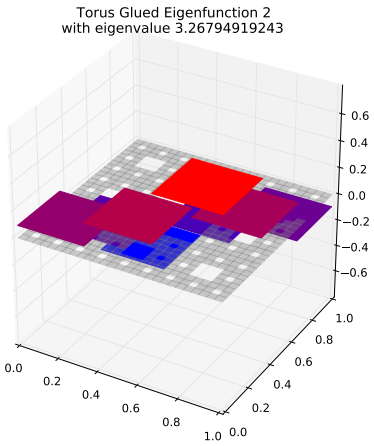
52 $M = 2$ Eigenfunction 51

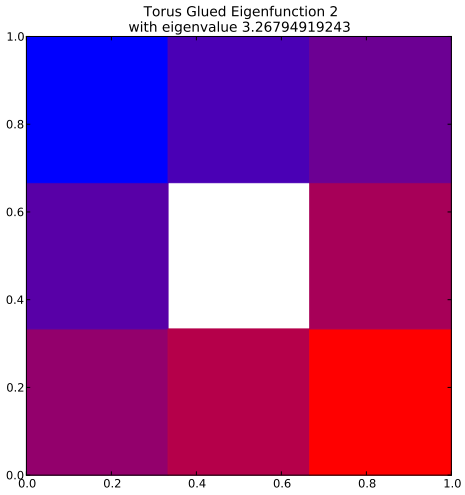
$M = 2$ Eigenfunction 51 has eigenvalue 6.00016431446





Compare to $m = 1$ eigenspace with eigenvalue 3.26794919243
(Note: Eigenspace Dimension > 1)

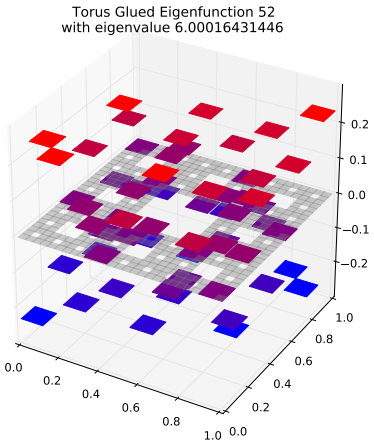


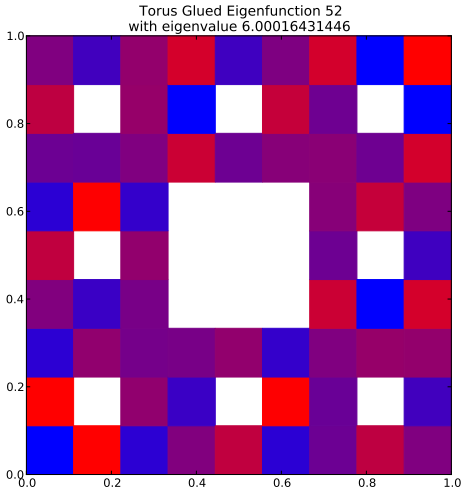


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 1.83606413721$
Dot Value: 0.25778074451686306

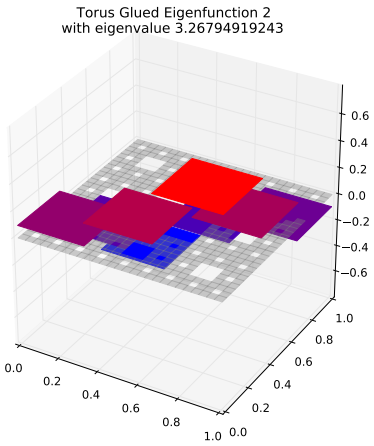
53 $M = 2$ Eigenfunction 52

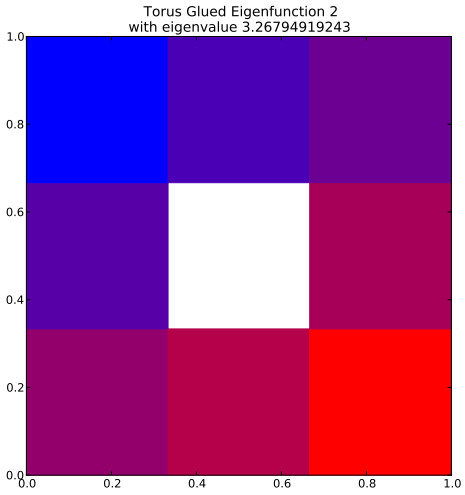
$M = 2$ Eigenfunction 52 has eigenvalue 6.00016431446





Compare to $m = 1$ eigenspace with eigenvalue 3.26794919243
(Note: Eigenspace Dimension > 1)

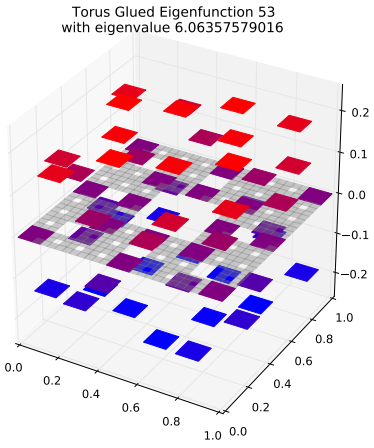


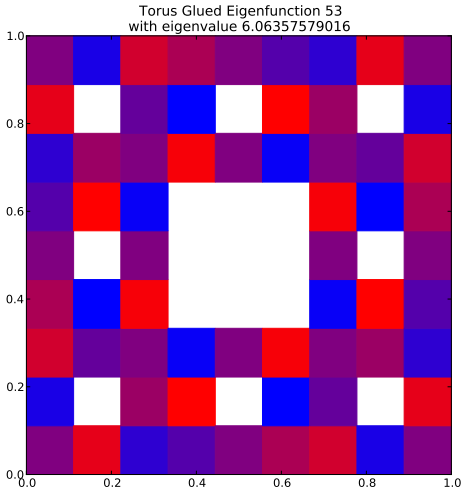


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 1.83606413721$
Dot Value: 0.2577807445168505

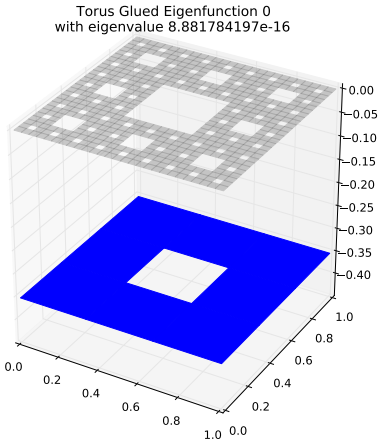
54 $M = 2$ Eigenfunction 53

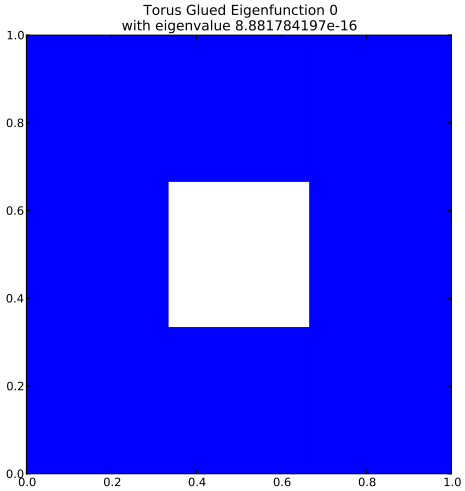
$M = 2$ Eigenfunction 53 has eigenvalue 6.06357579016





Compare to $m = 1$ eigenspace with eigenvalue 8.881784197e-16

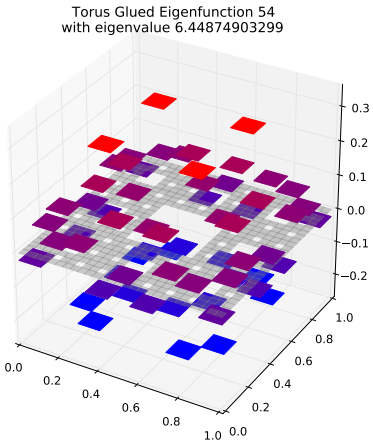


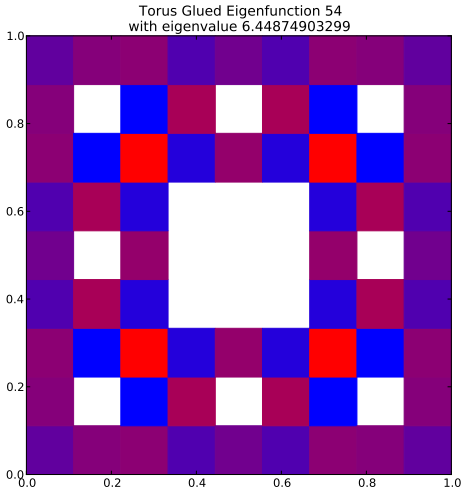


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 6.82697941727e + 15$
Dot Value: 2

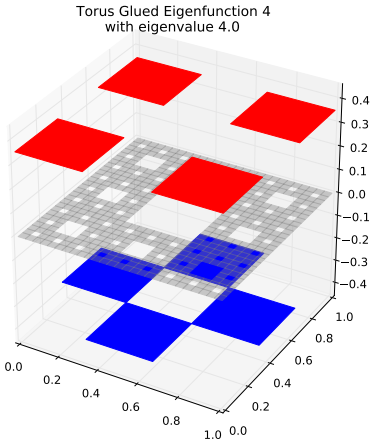
55 $M = 2$ Eigenfunction 54

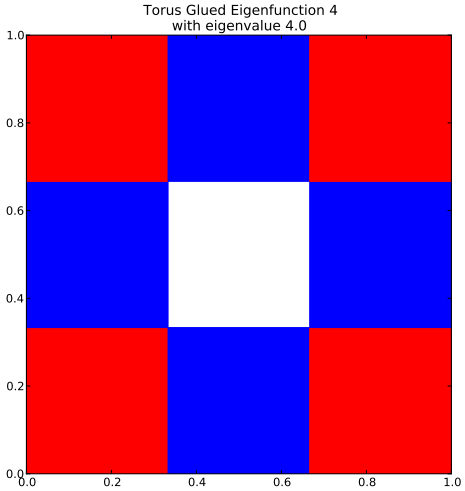
$M = 2$ Eigenfunction 54 has eigenvalue 6.44874903299





Compare to $m = 1$ eigenspace with eigenvalue 4.0

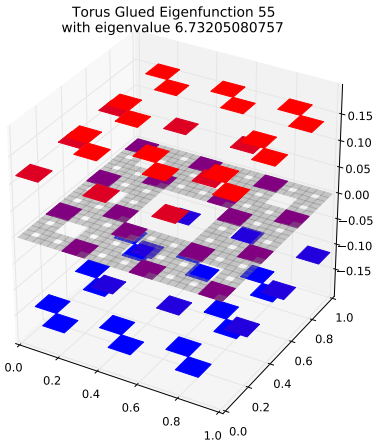


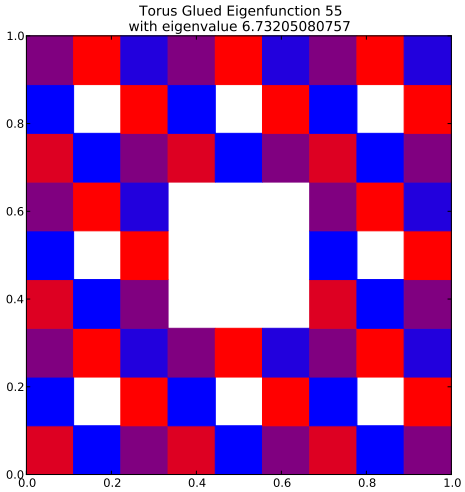


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 1.61218725825$
Dot Value: 0.0

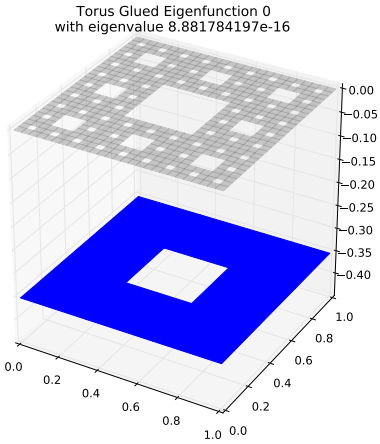
56 $M = 2$ Eigenfunction 55

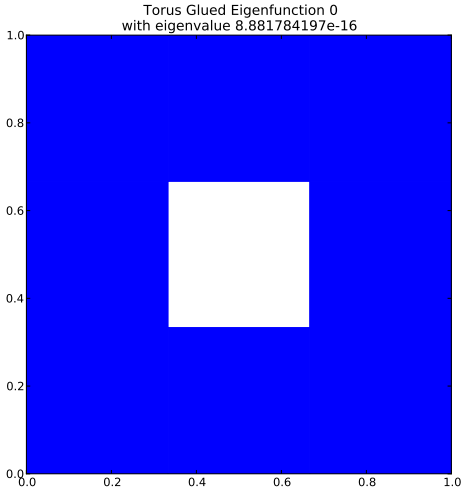
$M = 2$ Eigenfunction 55 has eigenvalue 6.73205080757





Compare to $m = 1$ eigenspace with eigenvalue 8.881784197e-16

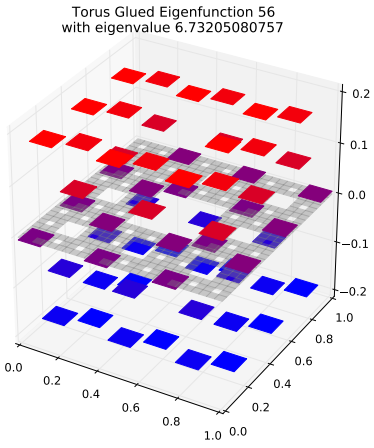


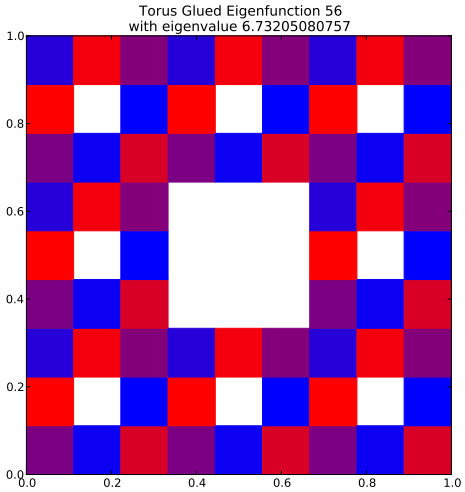


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 7.5796153771e + 15$
Dot Value: 2

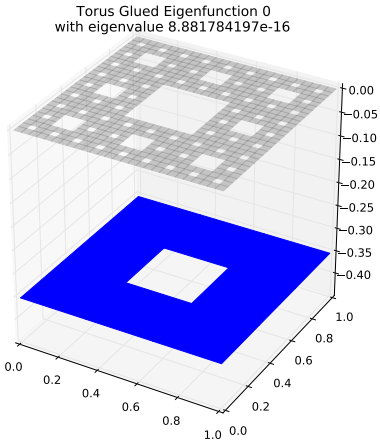
57 $M = 2$ Eigenfunction 56

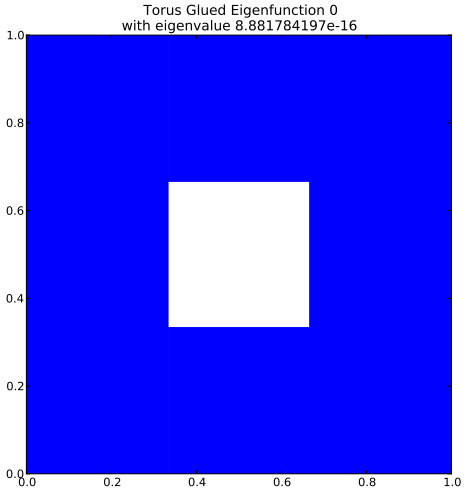
$M = 2$ Eigenfunction 56 has eigenvalue 6.73205080757





Compare to $m = 1$ eigenspace with eigenvalue 8.881784197e-16

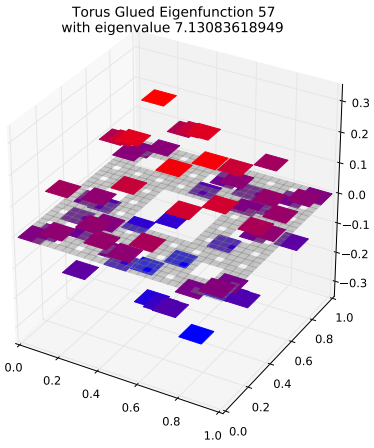


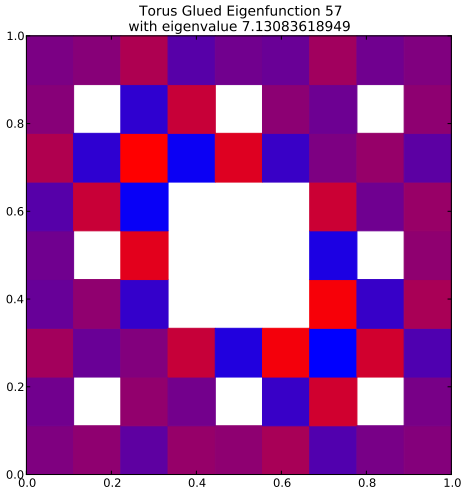


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 7.5796153771e + 15$
Dot Value: 2

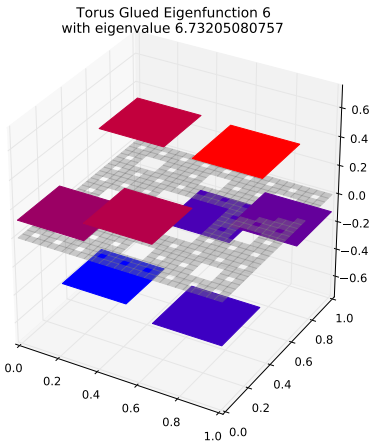
58 $M = 2$ Eigenfunction 57

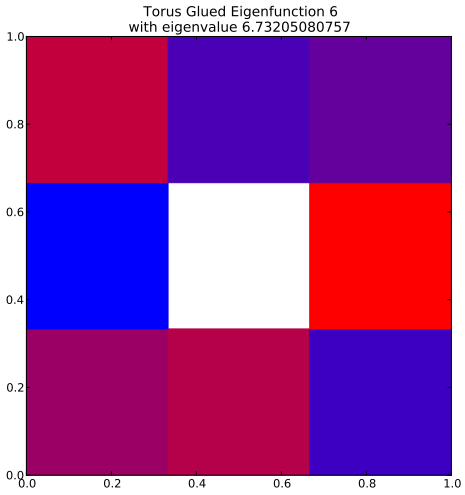
$M = 2$ Eigenfunction 57 has eigenvalue 7.13083618949





Compare to $m = 1$ eigenspace with eigenvalue 6.73205080757
(Note: Eigenspace Dimension > 1)

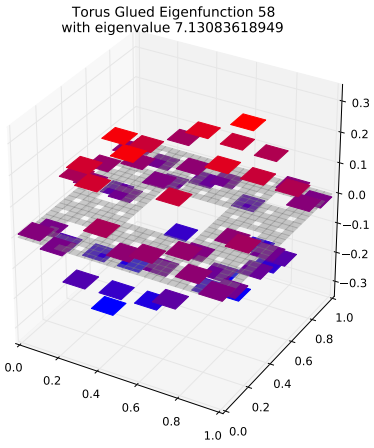


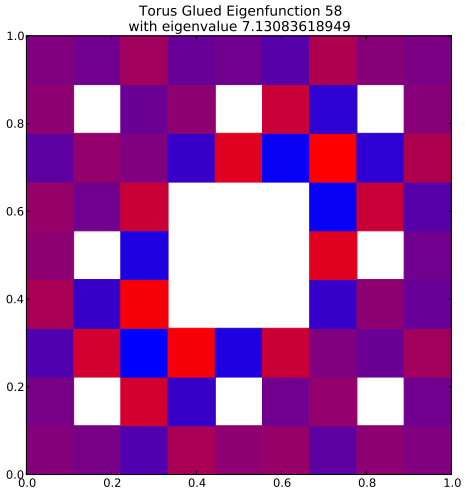


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 1.05923683485$
Dot Value: 0.0006700670542102438

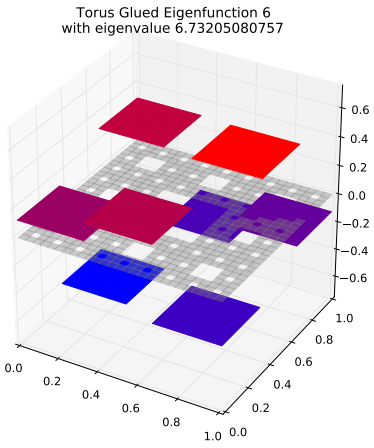
59 $M = 2$ Eigenfunction 58

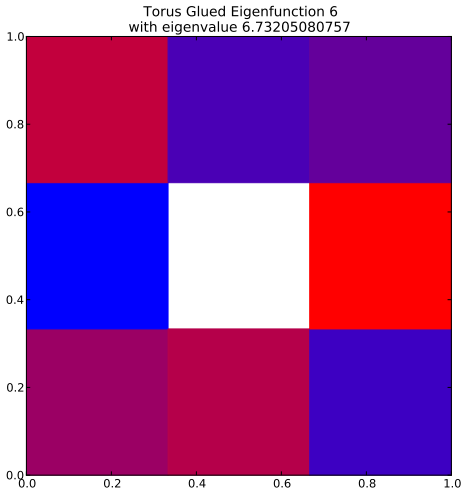
$M = 2$ Eigenfunction 58 has eigenvalue 7.13083618949





Compare to $m = 1$ eigenspace with eigenvalue 6.73205080757
(Note: Eigenspace Dimension > 1)

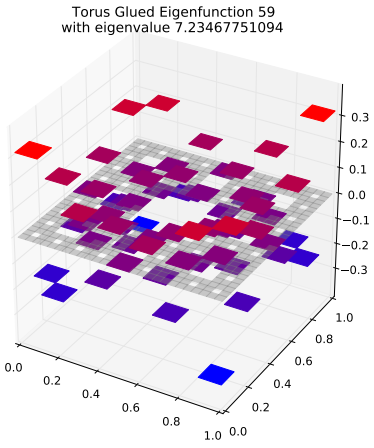


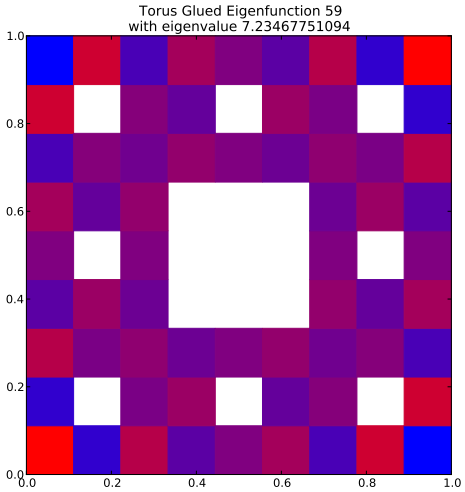


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 1.05923683485$
Dot Value: 0.0006700670542103548

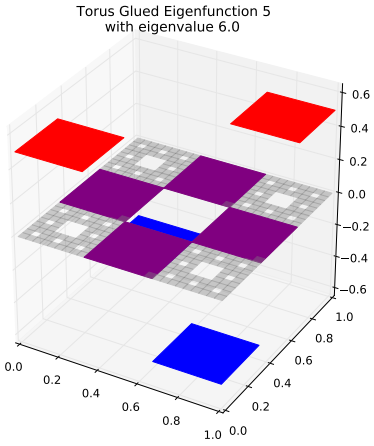
60 $M = 2$ Eigenfunction 59

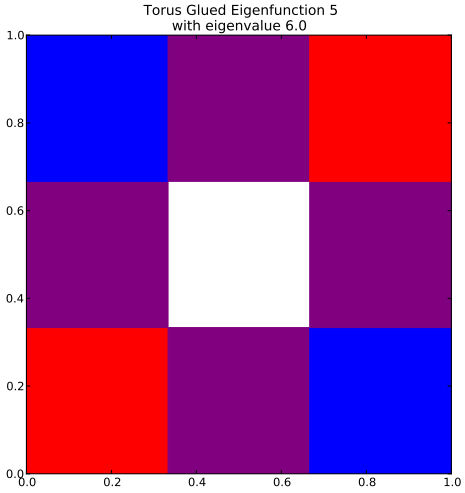
$M = 2$ Eigenfunction 59 has eigenvalue 7.23467751094





Compare to $m = 1$ eigenspace with eigenvalue 6.0

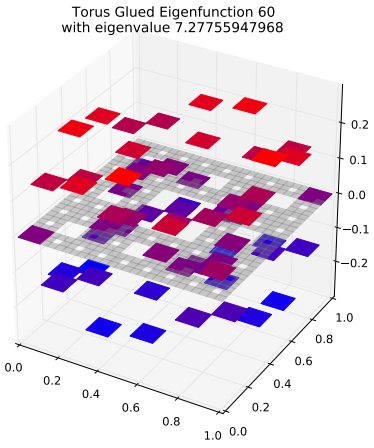


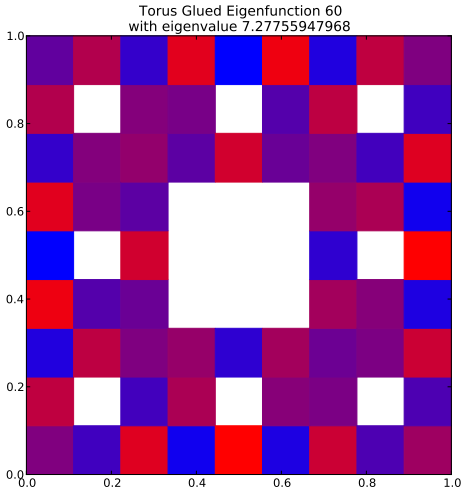


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 1.20577958516$
Dot Value: 2.220446049250313e-16

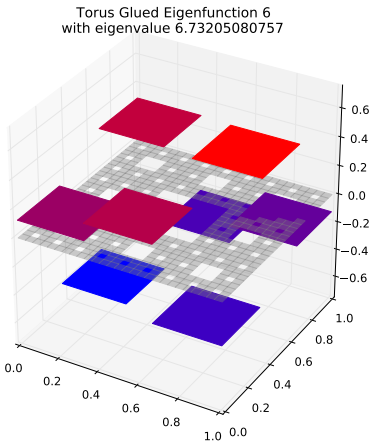
61 $M = 2$ Eigenfunction 60

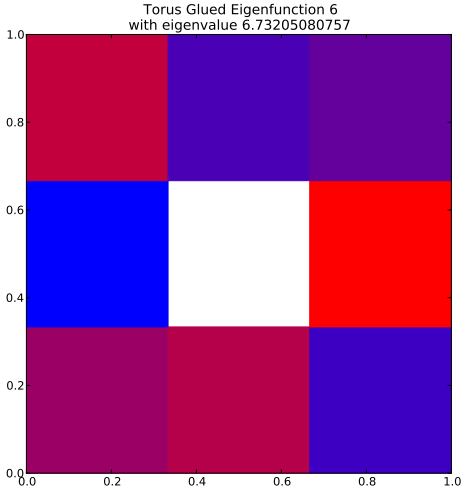
$M = 2$ Eigenfunction 60 has eigenvalue 7.27755947968





Compare to $m = 1$ eigenspace with eigenvalue 6.73205080757
(Note: Eigenspace Dimension > 1)

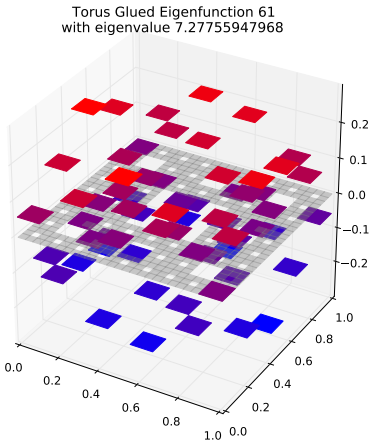


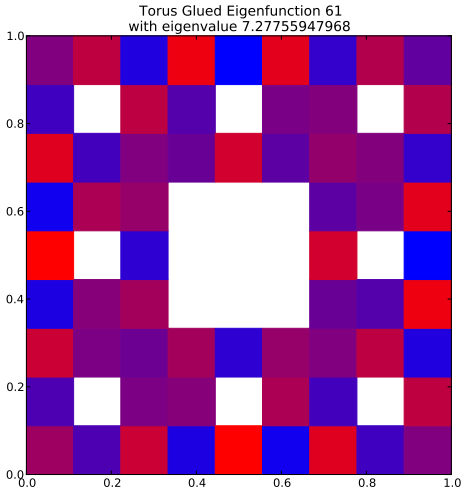


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 1.08103157384$
Dot Value: 0.008519342893784754

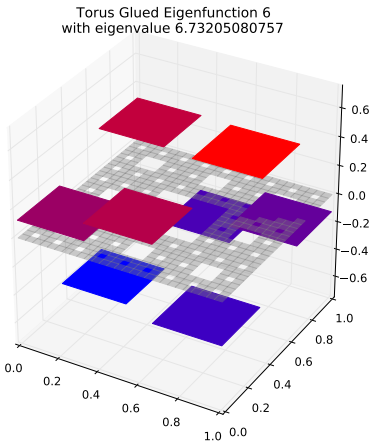
62 $M = 2$ Eigenfunction 61

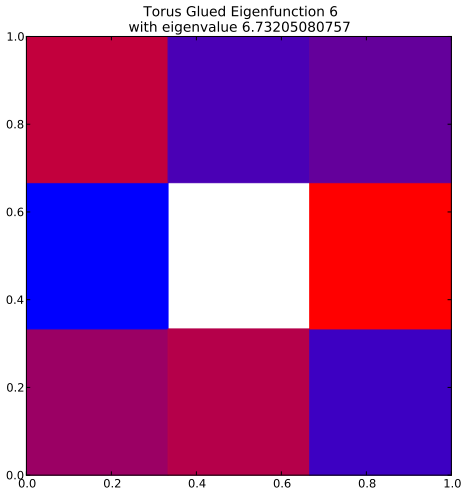
$M = 2$ Eigenfunction 61 has eigenvalue 7.27755947968





Compare to $m = 1$ eigenspace with eigenvalue 6.73205080757
(Note: Eigenspace Dimension > 1)

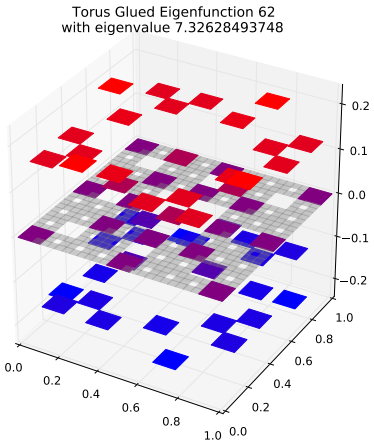


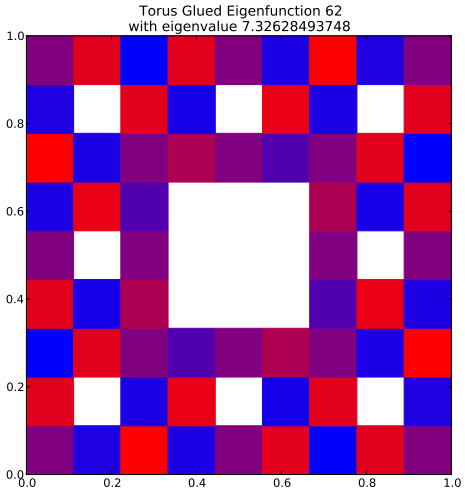


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 1.08103157384$
Dot Value: 0.00851934289378442

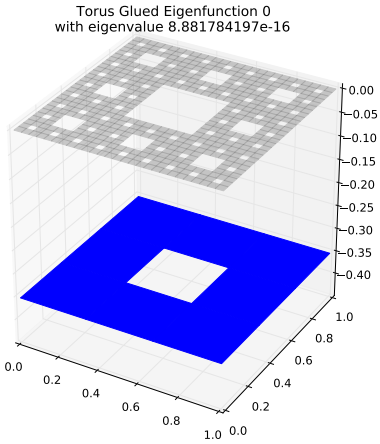
63 $M = 2$ Eigenfunction 62

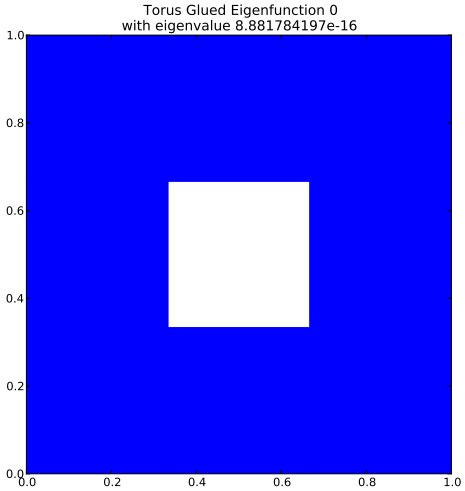
$M = 2$ Eigenfunction 62 has eigenvalue 7.32628493748





Compare to $m = 1$ eigenspace with eigenvalue 8.881784197e-16

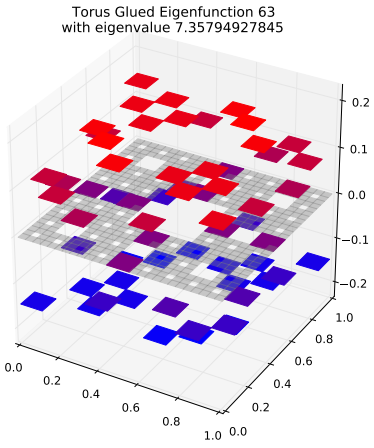


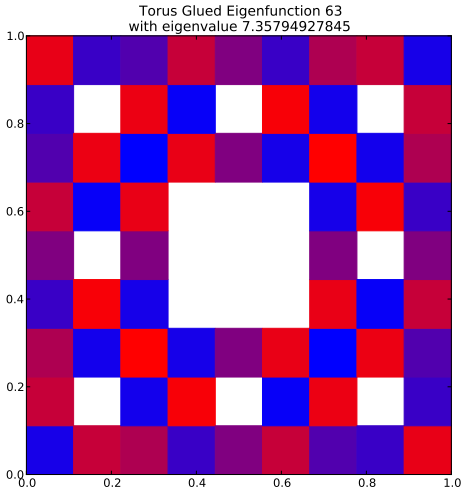


Eigenvalue Ratio: $\lambda_2/\lambda_1 = 8.24866352862e + 15$
Dot Value: 2

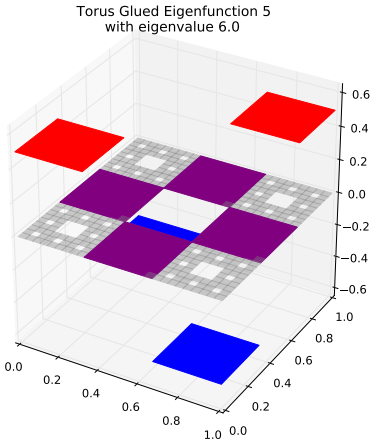
64 $M = 2$ Eigenfunction 63

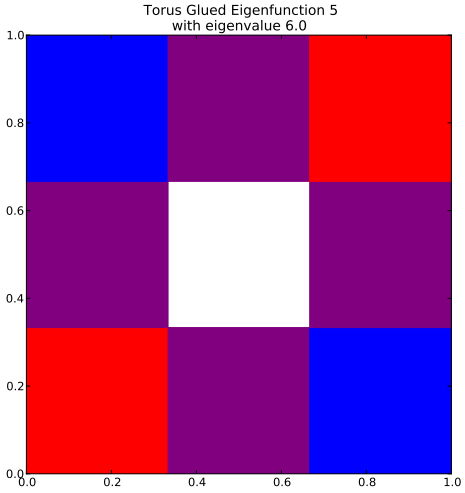
$M = 2$ Eigenfunction 63 has eigenvalue 7.35794927845





Compare to $m = 1$ eigenspace with eigenvalue 6.0





Eigenvalue Ratio: $\lambda_2/\lambda_1 = 1.22632487974$
Dot Value: 0.0