**1.** Use a quadratic form to compute continued fractions for the following pairs of numbers (see pages 20-21 of Chapter 2 for examples like these):

(a)  $(3 + \sqrt{6})/2$  and  $(3 - \sqrt{6})/2$  (b)  $(11 + \sqrt{13})/6$  and  $(11 - \sqrt{13})/6$ 

(c)  $(14 + \sqrt{7})/9$  and  $(14 - \sqrt{7})/9$ 

**2.** For the quadratic form  $x^2 - 14y^2$  do the following things:

(a) Draw the separator line in the topograph and compute the continued fraction for  $\sqrt{14}$ .

(b) Find the smallest positive integer solutions of  $x^2 - 14y^2 = 1$  and  $x^2 - 14y^2 = -1$ , if these equations have integer solutions.

(c) Find the linear fractional transformation that gives the periodicity translation along the separator line and use this to find a second positive solution of  $x^2 - 14y^2 = 1$ . (d) Determine the integers n with  $|n| \le 12$  such that the equation  $x^2 - 14y^2 = n$  has an integer solution. (Don't forget the possibility that there could be solutions (x, y) that aren't primitive.)

**3.** For the quadratic form  $x^2 - 29y^2$  do the following things:

(a) Draw the separator line and compute the continued fraction for  $\sqrt{29}$ .

(b) Find the smallest positive integer solution of  $x^2 - 29y^2 = -1$ .

(c) Find a glide-reflection symmetry of the separator line and use this to find the smallest positive integer solution of  $x^2 - 29y^2 = 1$ .

**4.** Compute the periodic separator line for the form  $x^2 - 43y^2$  and use this to find the continued fraction for  $\sqrt{43}$ .