

MATH 4370: Computational Algebra

## Problem Set 8

*Due Saturday, November 9, 2019*

You are allowed to work in groups, but the solutions you hand in should be written by you only.

If you did not receive a full score for a problem part you submitted, and would like to resubmit a new, corrected version, you can do so, within two weeks of the pset due date. Your final score on the pset will reflect the best score you received.

Instructions on how to hand in pset:

[https://gradescope-static-assets.s3-us-west-2.amazonaws.com/help/submitting\\_hw\\_guide.pdf](https://gradescope-static-assets.s3-us-west-2.amazonaws.com/help/submitting_hw_guide.pdf)

Cornell Libraries have free scanners, if needed:

<https://olinuris.library.cornell.edu/print-scan-wifi>

**Problem 1.** Given two ideal  $I, J \subseteq k[x_1, \dots, x_n]$ , express the varieties  $\mathbf{V}(I + J)$ ,  $\mathbf{V}(IJ)$ ,  $\mathbf{V}(I \cup J)$  in terms of the varieties  $\mathbf{V}(I)$  and  $\mathbf{V}(J)$ . Prove.

**From §3.1 of your book:** [Exercises 1, 2ab, 5, 6, 7](#)

You can use a computer algebra system for Exercise 7.

**From §4.3 of your book:** [Exercises 3, 4, 5, 6](#)

**From §4.4 of your book:** [Exercise 2](#)