Math 54 Worksheet 5 GSI: Lionel Levine 2/4/04

- 1. Describe the span of the vectors in  $\mathbb{R}^2$ .
  - (a) (1,0) and (1,1)
  - (b) (2,3) and (4,6)
  - (c) (1,0) and (0,1)
  - (d) (1, -1)
  - (e) (1, -1), (-2, 2) and (0, 0)

2. Describe the span of the vectors in  $\mathbb{R}^3$ .

- (a) (0, 0, 1) and (0, 1, 1)
- (b) (0,0,1), (0,1,1) and (1,1,1)
- (c) (1, 2, 3) and (3, 2, 1)
- (d) (1, 2, 3), (3, 2, 1) and (10, 10, 10)
- (e) (1, 1, 1), (-1, -1, -1) and (5, 5, 5)
- 3. Is it possible for one vector to span all of  $\mathbb{R}^2$ ? Why or why not?
- 4. Is it possible for two vectors to span all of  $\mathbb{R}^3$ ? Why or why not?

Bonus Problem (turn in on Monday for extra credit on the most recent quiz): Let

$$A = \begin{pmatrix} 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ 0 & 0 & 1 & 3 & 6 & 10 & 15 & 21 \\ 0 & 0 & 0 & 1 & 4 & 10 & 20 & 35 \\ 0 & 0 & 0 & 0 & 1 & 5 & 15 & 35 \\ 0 & 0 & 0 & 0 & 0 & 1 & 6 & 21 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 7 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}.$$

This matrix is called *Pascal's triangle*, and it is defined by the equations

$$a_{11} = a_{12} = \dots = a_{18} = 1$$
$$a_{21} = a_{31} = \dots = a_{81} = 0$$
$$a_{ij} = a_{i,j-1} + a_{i-1,j-1}, \quad \text{if } i \text{ and } j \text{ are } > 1.$$

Find  $A^{-1}$ .