Math 54 Worksheet 9 GSI: Lionel Levine 2/16/05

1. Find a basis for the given vector space, and find its dimension..

(a)
$$V = \{(x, y, z) \in \mathbb{R}^3 \mid x = 2y = -6z\}$$

(b)
$$W = \{(x, y, z) \in \mathbb{R}^3 \mid x + y + z = 0\}$$

(c)
$$W = \{(x_1, x_2, x_3, x_4, x_5) \in \mathbb{R}^5 \mid x_1 = x_2, x_3 + x_4 = x_5\}$$

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(d) $V = \{A \in M_{32} \mid A \begin{pmatrix} 1 \\ 1 \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}\}$

(e)
$$V = \{ p \in P_5 \mid p(x) = p(-x) \}$$